LECTURE NOTES ON FLUID MECHANICS

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TH-3 FLUID MECHANICS

Name of the Course: Diploma in Mech & Other Mechanical Allied Branches				
Course code:		Semester	4 th	
Total Period:	60	Examination	3 hrs	
Theory periods:	4 P/W	Class Test:	20	
Maximum marks:	100	End Semester Examination:	80	

A. RATIONAL:

Use of fluid in engineering field is of great importance. It is therefore necessary to study the physical properties and characteristics of fluids which have very important application in mechanical and automobile engineering.

B. COURSE OBJECTIVES:

Students will develop an ability towards

- Comprehending fluid properties and their measurements
- Realizing conditions for floatation
- Applying Bernoulli's theorem

C. TOPIC WISE DISTRIBUTION OF PERIODS

<u>Sl. No.</u>	<u>Topic</u>	Periods
01	Properties of Fluid	08
02	Fluid Pressure and its measurements	08
03	Hydrostatics	08
04	Kinematics of Flow	08
05	orifices, notches & weirs	08
06	Flow through pipe	10
07	Impact of jets	10
	Total Period:	60

D.CONTENT

1.0 Properties of Fluid

- 1.1 Define fluid
- 1.2 Description of fluid properties like Density, Specific weight, specific gravity, specific volume and solve simple problems.
- 1.3 Definitions and Units of Dynamic viscosity, kinematic viscosity, surface tension Capillary phenomenon

2.0 Fluid Pressure and its measurements

- 2.1 Definitions and units of fluid pressure, pressure intensity and pressure head.
- 2.2 Statement of Pascal's Law.
- 2.3 Concept of atmospheric pressure, gauge pressure, vacuum pressure and absolute pressure
- 2.4 Pressure measuring instruments Manometers (Simple and Differential)
 - 2.4.1 Bourdon tube pressure gauge(Simple Numerical)
- 2.5 Solve simple problems on Manometer.

3.0 Hydrostatics

- 3.1 Definition of hydrostatic pressure
- 3.2 Total pressure and centre of pressure on immersed bodies(Horizontal and Vertical Bodies)
- 3.3 Solve Simple problems.
- 3.4 Archimedes 'principle, concept of buoyancy, meta center and meta centric height (Definition only)
- 3.5 Concept of floatation

4.0 Kinematics of Flow

- 4.1 Types of fluid flow
- 4.2 Continuity equation(Statement and proof for one dimensional flow)
- 4.3 Bernoulli's theorem(Statement and proof) Applications and limitations of Bernoulli's theorem (Venturimeter, pitot tube)
- 4.4 Solve simple problems

5.0 Orifices, notches & weirs

- 5.1 Define orifice
- 5.2 Flow through orifice
- 5.3Orifices coefficient & the relation between the orifice coefficients
- 5.4 Classifications of notches & weirs
- 5.5 Discharge over a rectangular notch or weir
- 5.6 Discharge over a triangular notch or weir
- 5.7 Simple problems on above

6.0 Flow through pipe

- 6.1 Definition of pipe.
- 6.2 Loss of energy in pipes.
- 6.3 Head loss due to friction: Darcy's and Chezy's formula (Expression only)
- 6.4 Solve Problems using Darcy's and Chezy's formula.
- 6.5 Hydraulic gradient and total gradient line

7.0 Impact of jets

- 7.1 Impact of jet on fixed and moving vertical flat plates
- 7.2 Derivation of work done on series of vanes and condition for maximum efficiency.
- 7.3 Impact of jet on moving curved vanes, illustration using velocity triangles, derivation of work done, efficiency.

CHAPTERS COVERED UP TO IA- 1, 2,3,4

Learning Resources:

Sl No.	Name of the Book	Author Name	Publisher
1.	Text Book of Fluid Mechanics	R.K.Bansal	Laxmi
2.	Text Book of Fluid Mechanics	R.S khurmi	S.Chand
3.	Text Book of Fluid Mechanics	R.K.Rajput	S.Chand
4.	Text Book of Fluid Mechanics	Modi & Seth	Rajson's pub. Pvt. lt

** HLUID # MECHANICS

PROPERTIES OF FLUTDS =>

(1) Density on Mass Dunsity :-

- The mass of a fluid to its volume thus mass per unit volume of the mass of a fluid to its volume thus mass per unit volume of a fluid is called density. It is denoted by the symbol of (nho). The unit of mass density in SIL unit is key per cubic metre i.e. Key/m3.
- + The density of loguads may be considered as constant while that & gases changes with the variation of pressure and temperature.
- Mathematically, most density is written as $f = \frac{Mats \ of \ bluid}{Volume \ ob \ bluid} = \frac{M}{V}$

-> The value of density of voder is 1gm/cm3 are loop ug/m3.

Specific Weight on Weight Density :-

Aspecific weight on weight Density of a fluid is the nation between the weight of a blood to its volume. Thus weight per unit volume of a fluid is called weight density and it is denoted by the symbol W.

Thus mathematically, w= weight of bluid

Home, weight of bluid = mass of bluid × Acceleration due to gravity = mxg mass of bluid xg

=) Weight Density (w)= may = maes of fluid x g Volume of bluid

>[w= fg] = 3xg

+ The which it weight density in set which is Newton (m? .

-7 The value of specific weight on weight density (w) for water is 9-81 X1000 Newton Im3 in S.Z units.

[3] Specific Volume :--

-> Specific volume the a bluid is defined as the volume of a bluid is occupied by a unit mass on volume per unit mass of a bluid is called specific volume. Mathematically, it is expressed as

Thus specific volume is the necliprocal of mass density. 7 34 is expressed as malky. 7 34 is commonly applied to gases.

- Specific Gravity: --- Specific Gravity is defined as the notio of the weight density for density of a fluid to the weight density (on density) of a standard thuid. For lequids, the standard fluid is taken water and for gues, the standard fluid is taken air. Specific gravity is also called helative density. It is dimensionless quantity and is denoted by the symbol S.

Density of standard liquid = $\frac{fl}{fwg} = \frac{fl}{fwg}$ $\Rightarrow S = \frac{fl}{fwg}$ $\Rightarrow fl = S \times fwg$

of the specific greavity of bluid is known, then the density of the bluid will be equal to specific greavity of fluid multiplied by the density of water. For example, the specific greavity of meneury is 13.6, thence thensity of meneury = 13.6 × 1000 =15 Hg = 13.600 kg/m3.

-: VISCOSITY :-

- -7 Viscocity is defined as the property of a fluid which offens resistance to the movement of one layer of fluid over another adjacent layer of the fluid.
- + When two layers of a filural, a distance by apart, move one own the other at different velocities, say u and whole as shown in liquid, the Viscocity together with relative velocity Causes a shear stress acting between the fluid layers.
- -The top layer causes a shear stricts on the adjoirent lower layer while the lower of the dy the layer courses a shear stricts on the adjoirent top layer. This shear y du striess is proportional to the rate of velocity stringe is velocity with respect to y. It is denoted by symbol the strict velocity venilation thear is soled in Velocity venilation thear is soled in boundary
 - Muchangerally, ZX du of Z= H du -(1)
 - to interes 14 is the constant of proportionality and is known is the constant of proportionality and is known is the

du represente the rode of shear shain on note of shear

Representation on velocity greadient.
From equilities we have,
$$\mu = \frac{7}{\left(\frac{du}{dy}\right)}$$

Thus Viscosity is also defined as the Shear stress required to produce with rate of shear stream

Hence
$$T = \frac{V_{once}}{Nrea} = \frac{N}{1} \frac{1}{m^2}$$

$$\mu = \frac{V_{once}}{Nrea} + \frac{du}{dy}$$

$$= \frac{N}{m^2} \times \frac{dy}{du} = \frac{N}{m^2} \times \frac{m}{m/s} = \frac{N.s}{m^2}$$
SS unit of Viscopity = $\frac{Ns}{m^2} = \frac{Ns}{m^2}$.
SS unit of Viscopity = $\frac{Ns}{m^2} = \frac{Ns}{m^2}$.
Accelenation = Speed
 $\frac{Speed}{Sec}$
on Speed = $\frac{m}{sec}$ $x = \frac{m}{sec}$
 $-\pi g = \frac{m}{sec}^2$
than, $\mu = \frac{N \cdot s}{m^2}$ (Newton = mouss xaccelenation)
 $= \frac{N}{\mu} = \frac{kg \frac{m}{s^2} \times s}{m^2}$

The unit of Viscosity in Clips it also called poise which is equal to type-see.

The numerical conversion of the unit of Viscosity broom Mass with to class unit is given Below?

But 1 Newton = one kg (moss) x one
$$\frac{1}{Ser} \sum_{i=1}^{n} [acceleration]$$

= $\frac{1000 \text{ M} \times 100 \text{ Im}}{\text{Serl}}$ = 1000 × 100 $\frac{\text{Sm}}{\text{Sm}}$
= $1000 \times 100 \frac{\text{Sm}}{\text{Sm}}$
Thus fore Solving numerical providens, is viscocity it given
in poile, it must be divided by 1600 Im and $1500 \frac{\text{Sm}}{\text{Sm}}$
= $1000 \times 100 \frac{\text{Sm}}{\text{Sm}}$
=



In Chys units, Kinematic Uscessity is meleo known as stroke. Thus, one shoke = $cm^2/s = (\frac{1}{100})^2 m^2/s = 10^{-9}m^2/s$

Cantulake means = 100 Stoke

SURFACE TENSION AND CAPILLARITY 7

Surface Tension is debined as the tensile bare acting or the Surface of a loquid in contract with a gas one on the surface between two immiscible logards such that the contract subjace behaves like a membrane under tension. The magnitude of this borace per unit length of the bree surfrace will have the same value as the surface energy per unit and Of is denoted by Grock Vletter & (could signa). In MKS units, it is expressed as Kyt/m whele in st units as N/m.

SURFALE TENSION ON LIQUID DROPLET ?

Consider a small spherical droplet of a liquid of readins n. On the entire surface of the droplet, the tensile force due. to surface tension will be acting.

- Let &= surface tension of the liquid P = pressure intensity inside the droplet (in excess of the outside pressure intensity)

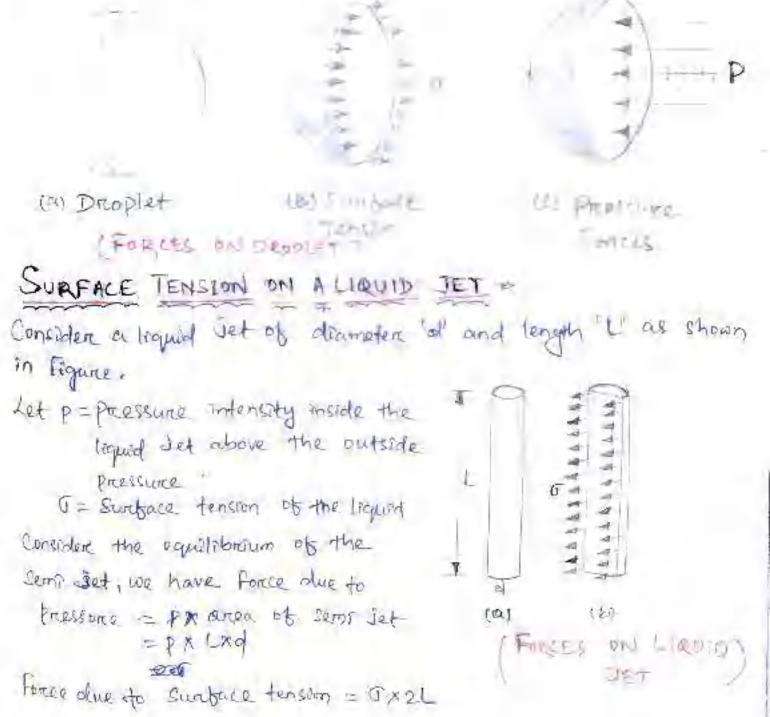
d = Dia of droplet het the droplet is cut into two trackes. The forces acting on one half (say left halt) will be

(1) Tensite force due to Surface tension acting anound the encumberance of the M Cut pontion as shown in bigure - and that is equal to = GX concumpenence - UXTO

(ii) Pressure borces on the area $\frac{\pi}{4}d^2 = p_X \frac{\pi}{4}d^2$ as shown in figure, These two borces will be equal and opposite under equilabrium conditions. The.

$$P = \frac{G \times \pi d}{\frac{\pi}{3} \times d^2} = \frac{4G}{d}$$

The above equation shows that with the decrease of diameter. of the droplet, pressure intensity inside the dropletincreases.



Equating the forces, we have $P \times L \times d = G \times 2L$ $= 7P = \frac{G \times 2L}{L \times d}$

SURFACE TENSION ON A HOLLOW BUBBLE 7

A Hollow bubble like a sonp bubble in air has two surfaces in contact with air, one inside and other outside. Thus two surfaces are subjected to surface dension. In such case, we have

$$P \Lambda \frac{\pi}{4} d^2 = 2x(0x\pi d)^2$$

$$\Rightarrow P = \frac{x \sigma \pi d}{\frac{\pi}{4} d^2} = \frac{x \sigma}{d}$$

-ICAPILLARITY =-

- r Captillarity is defined as a phenomenon of rule on fall of a liquid surface in a small tube relative to the adjacent general level of liquid when the tube is held vertically in the liquid. 7 The rule of liquid surface is known as Capillary rise while the fall of the liquid surface is known as Capillary rise while degression.
- -7 It is expressed indering of Cm on mm of liquid. Its value depinds upon the specific weight of the liquid, diameter of the tube and surface tension of the liquid.

Expressions for Capillanes Rise:-

Consider a glass tube of small diameter 'd' opened out both ends and is insended in a loquid, say wader. The loquid will rese in the tube above the level of the liquid.

Let h = height of the liquid in the tube : Under a state of equilibrium, the weight of liquid of height h is balanced by the force at the surdace of the liquid in the tube. But the porce at the surdace of the liquid in the tube, it the to surdace tension

The value of 0 between water and clean glass tube is approximately equal to zero and hence cas a is equal to writy. Then rise of water is given by

Expression for Capillany Fall :-

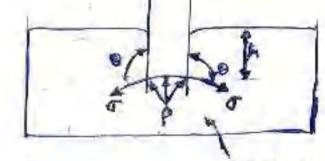
It the glass tube is alipped in mencuoy, the level of mencury in the tube will be lower than the general level of the outside loquid as shown in the figure.

Let hattleight of depression in tube

Then in equilibrium, two fonces are adding on the mercury inside the tube. First one is due to surface tension adding in the downward direction and is equal to FXId X Cos 0.,

Second bonce is due to hydrostatic bonce acting upwand and is equal to intensity of pressure at a depth h'x Area

Equating the two, we get EXTED X COSE = Pghx Zd² Th = 48 cose Pgd



... Value of 0 for mercury and glass tube is 1280. (CAPILLARY FALL)

FLUID PRESSURE AT A point 1 - [CHAPTER-02.] Consider a small Area dA in large mass of fluid. It the bluid is stationary than the force exercted by the Surrounding bluid on the area dA will diways be perpendicular to the surface dA. Let dF is the force suching on the area dA in the normal direction. Then the ratio of $\frac{dF}{dA}$ is known as the intensity of Pressure on Simply pressure and this reation is represented by p. Hence mothematically the pressure at a point in a bluid at west is $p = \frac{dF}{dA}$

inforce on pressure force, F= PXA.

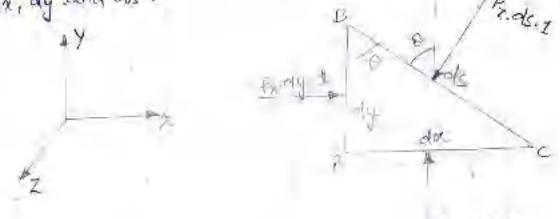
The web of pressure are liskyt /m2 and kyt/cm2 in MKS with sig Newton/m2 on N/m2 and N/mm2 in SI units N/m2 is known as pascal and is represented by Pa. other commonly used units of pressure are:kpa = kilo parcal = 1000 N/m2-· bar = 100 kpa = 10 N/m2.

PASCAL'S LAW 7

It states that the processure on intensity of preserve at a point in a static fluid is equal in all olinections. This is proved as:

10

The fluid element is of very small dimensions.



(FORCES ON A FLUID ELEMENT)

Consider an arbitrary blued element of wedge shape in a blued made at rest as shown in figure. Let the weight of the element perpendicular to the plane of paper is unity and pr by and Pr one the pressures on intensity of pressure acting on the force AB, AC and BC respectively. B Let LABL = D, then the forces acting on the element are: (1) Pressure forces moremal to the surfaces and (2) Weight of element in the vertical direction. The forces on the forces are: Force on the forces AB = Pr X Area of force AB = Presdy X1

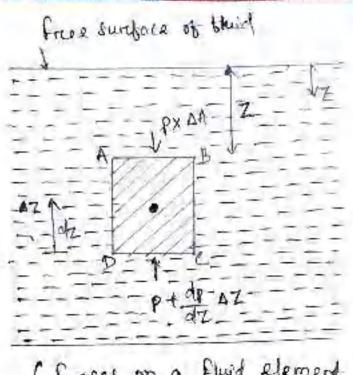
Similarly torce on the face AC = Pyx dx X I forece on the face BC = Pz x ds x 1 weight of element = (Mals of element) x of = (Nolume xp)xg = (MaxACx+)xpxg where P= density of bluid Resolving the borces in X-direction, we have Px Xdy X1 - P(ds X1) sin(900-0) = 0 Px X dy X 1 - Pzds X L Cos D = 0 March. on But from bigune, ofs coso = AB = dy Px xdy x1 - Pz xdy x1 = 0 $P_X = P_Z$ on similarly, resolving the borces in Y-direction, we get Pyxdxx1-pzxdsx1005(900-0) - dxxdy x1xfxg=0 + py dx - pz ds strie - du dy x g xg = 0 10R/1 Let the width of the elements is 1. Hence the onea of force to an face AB = dy x 1 (FAB = Pyxdyri) area of force on force AC = daix1 (FAC = paxdax1) anea of bonce on face BC = ols XI (FBC = PZ XdsXI) Weight of element = (mass of element) is g = f x Valums xg = Px (ALX ABX1) Xg For equilibrium considering the body at equilibrium Resolving the left and night forces

FAB = FBC (25 D -> Py dy & = Pz ds 1 cos 0 + Py dy = Pz.dc tos a + cos 19 = 13 × 14 de to ds Los & t dy Applying this in the equilar pyidg = Pz dg -> Py = Pz -Resolving the up boreds and door boreas FAC = FBL SIT & + 10 => Px dx-1= Pz ds 1. 100+ + + (1/2-+ dy-1) × 3 => Pa. dx = Pz ds sir 0 + gg dx dy as dx dy will be very small. Hence 4 ion be neglected. Applying in the expection Px. dx = Bz dx => Px = Pz Pa=Py=Pz @ PRESSURE FLEAD & HYDROSTATIC LAW SH

The pressure at any point in a fluid at rest is obtained by the Hydrostatic Law with states that the reaks of increase of pressure in a ventical observiced direction must be equal to the weight density of the fluid at the points

Ist ΔA = Looss Sectional Acta ΔZ = Haight of bluid element P = pressure on face AB Z = Distance of bluid element from brue surface W = Weight distrity of bluid

۴.,



(forces on a fluid element)

for equilibrium

$$\begin{aligned}
 & D + (P \times \Delta A) = (P + \frac{dP}{dz} \Delta Z) \Delta A \\
 = \int f(\Delta A + \Delta Z) g \end{bmatrix} + P * \Delta A = (P + \frac{dP}{dz}) \Delta Z \cdot \Delta A \\
 = 1 - \int \Delta A \cdot \Delta Z g + P \cdot \Delta A = P \Delta A + \frac{dP}{dz} \cdot \Delta Z \cdot \Delta A \\
 = 1 - \int \Delta A \cdot \Delta Z g + P \cdot \Delta A = P \Delta A + \frac{dP}{dz} \cdot \Delta Z \cdot \Delta A \\
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 = 1 - \int A \cdot \Delta Z g = \frac{dP}{dz}
 = \frac{dP}{dz} \cdot \Delta Z \cdot \Delta A
 = 1 - \int A \cdot \Delta Z g = \frac{dP}{dz}
 = \frac{D}{dz}
 = \frac{D$$

This equation is known as Hydrostatic Law. de = tg $\left(\frac{1}{2} = \frac{P}{P_2}\right)$ => Sdp= Stgdz >> P= fgz

TYPES OF PRESSURES 1-

- The pressure on a fluid is measured in two different systems. In one system, it is measured above the absolute Zerio on Complete, Vacaum and it is called the cubsolute pressure and in other system pressure is measured above the atmosphereic pressure and it is called gauge pressure. There are different types of pressure in the system.
 - @ Absolute pressure
 - & Gauge pressure
 - 3 Vacuum pressure
 - (2) Absolute Pressure ?

let is defined as the pressure which is measured with the

(3) Grange PRESSURE =>

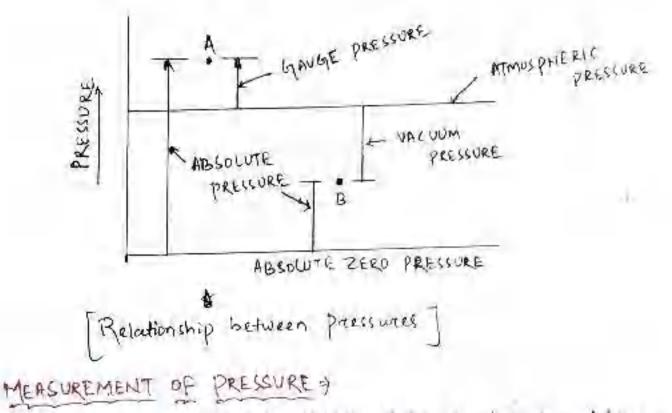
It is defined as the pressure which is measured with the help of a pressure measuring instrument, in which the atmospheric pressure is taken as clatum. The atmospheric pressure on the scale is marked as Zeno.

(1) Vacuum pressure of

It is defined as the pressure below the atmospheric pressure.

The relationship between the absolute pressure gauge. Pressure and vacuum pressure are shown in figure bolow. Mathematically.

(i) Absolute pressure = Gauge pressure + Atmosphenic on Pals = Patin # Pgauge (ii) Vacuum pressure = Atmospheric pressure - Absolute pressure => Pval = Patm - Pab



The pressure of a fluid is measured by the following devices: 1. Manometers 2. Mechanical Gauges

(1) MANOMETERS 7

Manometers are defined as the devices used for measuring the pressure at a point in a fluid by balancing the column of fluid by the same on another column of other fluid. They are classified as :-

(a) simple manomedens (b) Dobberential Manomedens

(3) MECHANICAL GAUGES 9

the pressure by balancing the build column by the spring on dead weight. The commonly used mechanical pressure gauges are :-

(a) Diaphragen pressure gauge (c) Dead-weight pressure gauge (b) Bourdon tube pressure gauge (d) Bellows pressure gauge PROBLEMS ? @1 Catculate the density, specific weight and weight of 1 CATCULATE the density specific greavity 11.7 ? 1 CH & Petrol of specific greavity 11.7 ?

$$\begin{split} & \underset{W=2}{\overset{W=2}{12}} & \underset{W=2}{\overset{W=2}{12}} \\ & \underset{W=2}{\overset{W=2}{12}} \\ & \underset{W=1}{\overset{W=1}{12}} \\ & \underset{W=1}{\overset{W=1}{12}$$

(<u>9.3</u> Two horizontal plate when place 1.25 cm apart from each other & the space between them is filled with oil of the viscosity 14 poise. Calculate the shear stress in Oil & is the upper plate is moving with a velocity of 2.5 m/s.

(Anto

$$\frac{M_{2}}{N} = \frac{1}{25} cm = \frac{1}{25} \times 10^{-2} m$$

$$N = \frac{14}{10} poise = \frac{1}{10} \frac{1}{10} = \frac{1}{4} \frac{1}{10} \frac{1}{2} \frac{1}{10}$$

$$\frac{1}{10} = \frac{1}{10} \frac{1}{10} = \frac{1}{10} \frac{1$$

Q:3 Find the kinemetic Viscosity & specific gravity of an oil having density of 981 kg/m3. The shear stress at a point in oil is 02452 N/m2 & velocity gradient is given by 0.2/sec.
(Huy) for 981 kg/m3 V = 7 T = 0.2452 N/m2 S = 7

 $\frac{du}{dy} = 0.2/sec$ $V = \frac{44}{7}$ $\Rightarrow \mu = \pi/\frac{du}{dy} = \frac{0.2452}{0.2} = 1226 \text{ NS}/m^2$ V = 4/9 $= \frac{1226}{901} = 0.001249 \text{ m}^2 \text{ s}$

Q.4 The welocity distribution for flow over a flat plate is given by $U = 3/4 y - y^2$ in which U is the velocity in m/s 2 y is the distance in metric above the plate Determine the shear stress at y = 1.5 m & the dynamic viscosity at 8.6 poile.

(Ant)

: SIMPLE MANDMETERS :

A simple manometer consists of a glass tube having one of its ends connected to a point where pressure is to be measured and other and remains open to admosphere. Common types of simple manometers are:-(1) prezometers.

(3) U-tube manometers and

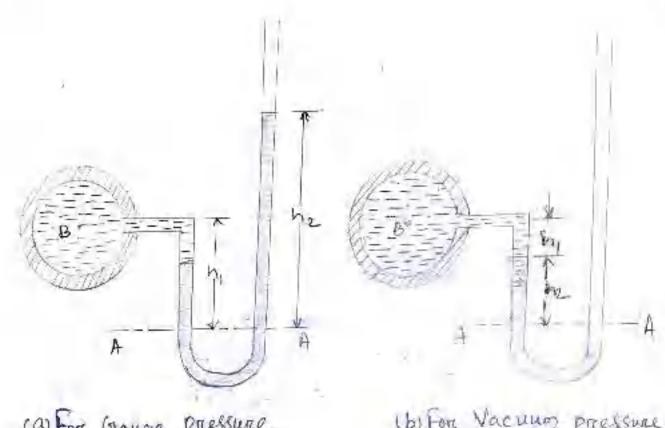
(3) Single Column manometers.

(1) PLEZOMETER 7

It is the simplest boars of manometer used for newsuning gauge pressures. Die end of this manometer is connected to the point where precisive is to be measured and other end is open to the almosphere of stown in bigune. It at he rise of logoid gives the Brekkine head at that point. It det a point A, the height of loguid say who water is h in pressure at the $A = p \times q \times h \frac{N}{m^2}$.

(2) U-TUBE MANOMETER =>

"It consists of glass tube bent in U-shape, one-end of which is connected to a point at which potessure is to be measured, and other end remains open to the atmosphere as shown in \$ the figure. The tube generally contains mercury or any other liquid whose specific gravity is greater than the specific gravity of the lequid whose pressure is to be measured.



(a) For Gauge pressure

(b) For Vacuum pressure

(1) FOR GAUGE PRESSURE =7

Let B is the point at which pressure is to be mensured, whose value is p, the datum line is A-A.

het his height of light liquid above the dotum line has height of heavy loqued above the datum line SI = Specific granty of light liquid fin Density of light liquid = lovox s, Sz = Specific gravity of heavy liquid B= Denvity of heavy liquide love XS2

As the pressure is the same bon the horizontal surface, How pressure above the heatzontal datum line A-A in the left cour and in the regist column of V-lubic manometers. Should be s Pressure above A-A in the rept column = P+ f+xgxh, Pressure above A-A mithe reight column = PIX JXh2

Hence reputing the two prossures. P+Pigh = Pzghz シア= わっわっ -- い

(B) FOR VACUUM PRESSURE =)

For measuring vacuum pressure, the level of the heavy loquid in the manometer will be as shown in the above brighter.

Then pressure above 4.4 in the left column = fight fight p pressure head in the right column above A-A = 0

1. Hence Pzghzt figh, +P=D > P=-#23 h2+ fighi) ----(2)

[3] SUNALE LOLUMN MANOMETER =>

Single Column manameter is a modified born of a U-tube manometers in which a reservitors thaving a large cross-sectional area (about too times) as compared to the area of the tube is connected to one of the limbs (say left (mb) of the manometer as shown in figure. Due to large exoss-sectional area of the reservion, bon any variation in pressure, the change in the liquid level in the neservoir will be very small which maybe neglected and thence the pressure is given by the height of loguid in the other limb. The other limb may be vertical or inclined. Thus there are two types of single tolumn manometers as: (1) Vertical single column manuneter

(2) Indined single column mariometers

(1) VERTICAL SINGLE COLUMN MANDMETER "7

The bigurce shows the Vendrical single column manometer, Ket X-X be the datum line in the reservolik and in the right line of the manometer, when it is not connected to the pipe, when the manometer is connected to the pipe, due to high pressure at A, the heavy located in the reservolik will be pushed downway and will resc in the right limb.

hz = Rose of heavy lequilat in roight lamb

- hr= Height of centre of pipe.
- PA=Pressure at A, which is to be measured
- A Cross. sectional Area of the reservolue
- a = Crease-sectional area of the reaght lamb
- Si=spignavity of lequid in pipe-
- Sz= sp. gravity of heavy liquid in reservor and right Himbs
 - Pi = Dansity of lequild in pope-
 - to = Density ob- Logard in meser would

Ealt of heavy liquid in reservice will cause a ruse of heavy liquid level in the right limb,

kη

RESERVOIR

X

$$A \chi \Delta h = \alpha \chi h_2$$

$$\Rightarrow \Delta h = \frac{\alpha \chi h_2}{A} - c b$$

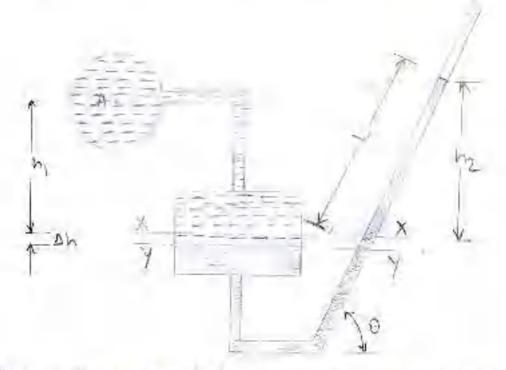
Now consider the datum line Y-Y as shown in bigune, then pressure in the right timb above Y-Y.

Pressure in the left limb above Y-Y = fix gx (ahthi) + PA

Equating the pressurve; we have $f_2 \times g_X(Ah+h_2) = P_1 \times g_X(Ah+h_1) + P_A$ = $P_A = -P_2 g_1(Ah+h_2) - P_1 g_1(Ah+h_1)$ = $Ah(P_2 g_1 - P_1 g_1) + h_2 P_2 g_1 - h_1 f_1 g_1$ Eut from equation (i): $Ah = \frac{a_X h_2}{A}$ $\Rightarrow P_A = \frac{a_X h_2}{A} = [P_2 g_1 - f_1 g_1] + h_2 f_2 g_1 - h_1 f_1 g_1 = \infty$ As the area A is berry large as compared to a hence tration $\frac{A}{A}$ becomes very small and can be neglected. Then $P_A = h_2 f_2 g_1 - h_1 f_1 g_1$ from A by undown with its clean that as h_1 is known and hence by knowing h_2 on wave of heavy laggerid in the rought lamb, the

pressure at A can be pregtected Calculated.

[3] INCLINED SINGLE COLUMN MANOMETER +



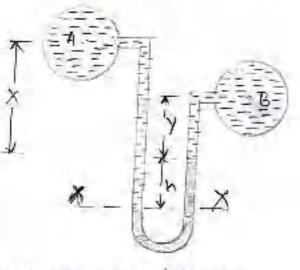
The bigune shows the inclined single column manumeters. This manameters is more sensitive. Due to inclination the clustance moved by the heavy liquid in the roight loops will be more. Let L= Length of heavy loquid moved inreight limb broom X-X 0 = Inclination of right limb with hurszontral he = Ventical rise of heavy loquid in right limb from X-X to Friend equation, the precisine at A-15 PA= h2f2g - hifig substituting the value of hz, we get PA= Smox f2g-hifig

- DIFFERENTIAL, MANDMETERS :-

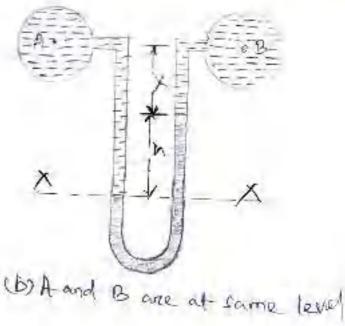
Differential manometers are the devices used for measuring the distremence of pressures between two points in a pipe on in two dotterent pipes. A differential monormater consists of a lotube, containing a heavy liquid, whose two ends are connected to the points, whose difference of pressure is to be measured. Mosil comming types of differential manometers are :-(1) U-tube dokkerential manometer and (3) Envented U-tube differential manameters.

(1) U-TUBE DIFFERENTIAL MANDMETER 7

The figures shows the differential manometers of U-tube type.



Cay Two pipes ad disbarrent levels



In bigure casthe two points A and B are at disperent level and also content logenits, of disperent specific gravity. These points are connected to the U-tube disperential manuncles. Let the pressure at A and B are Pa and Pa

- Let h= toppenence of meaning level in the U-tube
 - y = Distance of the centre at Bitmon the morecurry level in the night limb
 - X= Distance of the control of A, brow the marcany level in the night limb
 - Pi = Density of liquid of A
 - fz = Density of loquid at B
 - fy = Density of heavy leght of mercany
- Taking datum line of X-X.
- Prossure above X-X in the left limb = fig (h+x) + Pr
 - where PA = Pressure at A.
 - PRESSURE above X-X in the night limb = fox 3x h + fox 7x y + po where Pa = pressure of B.
- Equating the two pressure, we have
 - $f_1g(h+x)+P_A = f_3x_3xh+f_2gy+f_B$ $= 1P_A - P_B = f_3x_3xh*+f_2gy - f_1g(h+x)$ $= h \times g(f_g-f_i)+f_2gy - f_1gy$
 - Difference of pressure at A and B =
 - hx9(fg-fi)+f29y-figx

In Figure (b), the two points A and B are all the same level and contains the Same liquid of density fi, then pressure above X-X in right limb = fg X g X h they X 2++ pg pressure above X-X in right limb = fg X g X h they X 2++ pg

Equating the two pressure

$$f_g \times g \times h + P_1 g \times + P_8 = f_1 \times g \times h + x) + P_4$$

 $= P_A - P_8 = f_g \times g \times h + f_1 g \times -f_1 g (h + x)$
 $= g \times h (-f_1 - f_1)$

2] INVERTED U-TUBE DIFFERENTIAL MANDMETER-=> De consists of an invended U-elube containing a light liquid. The two ands of

the tube are connected to the points where difference of pressure is to be measured. 24 is used for measuring difference of low pressures. The bigure shows on inverted U-tube difference of B. Connected to the two points A and B test Let the pressure at A is more than the pressure at B. Let his height of liquid on left links below the detuntione X-X h= Difference of liquid in numberlimb Xh= Difference of liquid at A fis = Density of liquid at A fis = Density of liquid at A Pa = pressure at A-



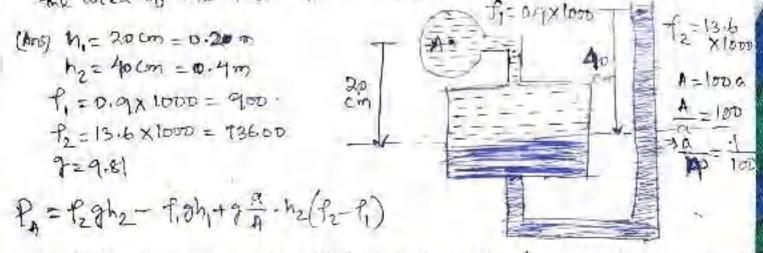
Taking X - X as datum line then pressure in the left limb below X - X= $P_A - P_F X g \times h$,

Pressure in the night limb below X-X = RB- P2×9×h2-Ps×9×h

B = pressure at B

Equating the two pressures $P_{a} - P_{i} \times g \times h_{i} = P_{a} - P_{2} \times g \times h_{2} - P_{5} \times g \times h$ $\Rightarrow P_{a} - P_{B} = -P_{i} \times g \times h_{i} - P_{2} \times g \times h_{2} - P_{5} \times g \times h$ Questions]

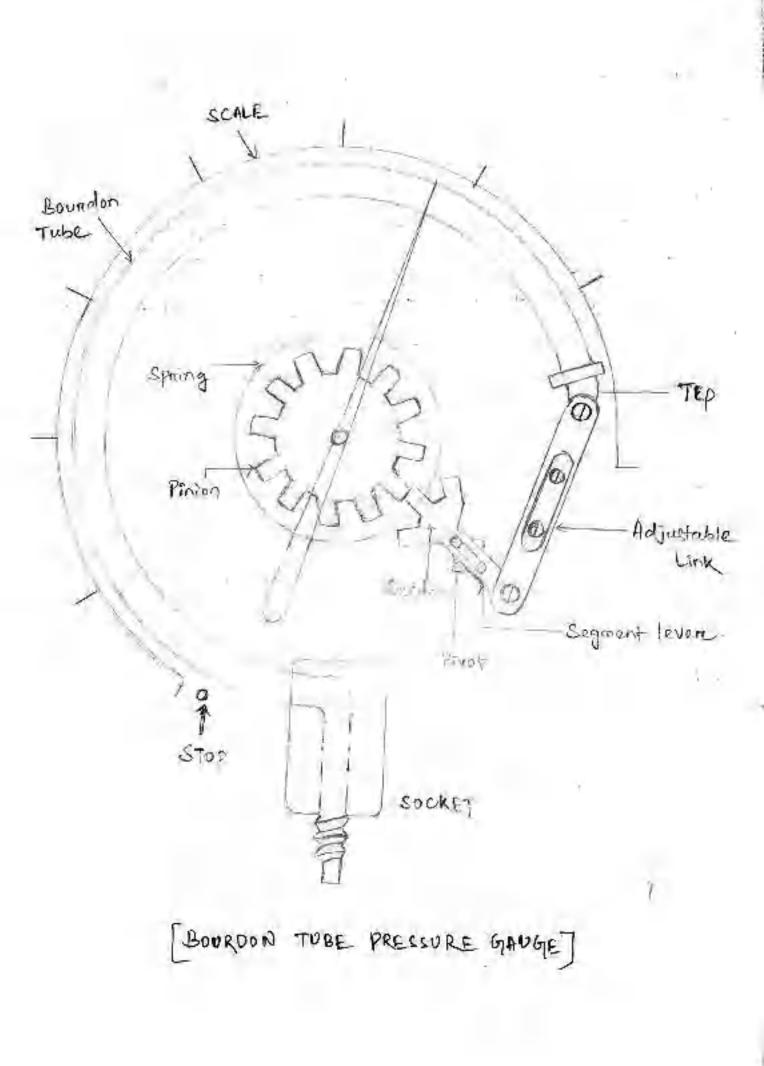
- (1) A simple U-tube monomater is used to managine the pressure of worker, in a pipe the which is above the straighteric pressure. The contact between whee big determine the pressure of the 20 m the main line is the little entry more the level of the intervent the limb of U-tube is local and the face surface of the the limb of U-tube is local and the face surface of the the is out the same keel as the center of the pipe? Ans) PATPI Thi = P. The spat(1000 x 9.81 x 10 x 10⁻²) = (13.6 × 1000 x 9.81 x 100x (r 2)) are 1000 at 100 and 100 x 9.81 x 100x (r 2) are 10000 at 100 at 100 x 9.81 x 100 x 9.81 x 100 x 10.2) are 10000 at 100 at 100 x 9.81 x 100 x 9.81 x 100 x 10.2)
- (3) A single column monometer is connected to a pope containing a liquid of specific gravity and an enough the figures. Find the pressure on the pope is the area of the restancian is looting the area of the tube of manometer ?



- = 13600x9.81x0.4-900x9.81x0.21+ 9.81×100 ×0.4 (13600-900) = 53366.4-17658+0.03924×12700
 - = 35,708.9 +498.348
 - = 36206-748 N/m2 (Hrs)

BOURDON TUBE PRESSURE GAUGE

- 7 Bourcolon tube pressure gauges one classified of mechanical pressure measuring instruments, and thus openate without any electricical power. This type of pressure gauges were first developed by E. Boundon in 1849.
- 7 Boundan tubes and madially formed tubes with an oval emoss-confirm.
- -7 Boundon tobo pressure granges can be used to measure over a wide manye of pressure boom variant to pressure as high as bed thousand psi.
- 7 It is basically consisted of a C-shaped hollow tube, whose one and is fixed and connected to the pressure tapping, the other and free .
- -7-The Cross section of the tube is elliphical, when pressure is applied, the elliphical tube (Bounder tube) takes to acquire ra cincular cross-section, as a result, stress is developed and the tube trues to Streighter up.
- magnitude is pressure.
- This motion is the measure of the pressure and is indicated via othe movement of a deblecting and indicating mechanism is attached to the force and that metates the pointer and indicates the pressure reading.
- and Benylloum, Copper.
- -1 Though the C-type tubes are most common, other shapes et the tubes, such as helocal, twisted or spircal tubes are also in use.



CHAPTER - 03

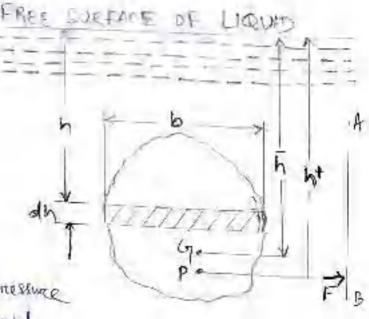
TOTAL PRESSURE AND CENTRE OF PRESSURE -)

- or Total pressure is defined as the force exercted by a staticity on a sunface either plane on Curived when the blacid comes in contact with the sunfaces. This force always acts normal to the Sunface.
- "7 Centre of pressure is defined as the point of application of the total pressure on the surface. There are four cases of submary surfaces on total the total pressure force and centre of pressure is to be determined. The Submerged surfaces may be (1) Vertical plane surface (2) Horizontal plane surface (3) Inclined plane surface
 - (4) Curved surface

(1) Ventical plane surface submerged in Liquid =7

Consider a plane Vertical suntaine of curbitrary shape immension

- Let A = Total area of the surgace
 - h T Distance of C.G. of the curea brown breez surface of loguid
 - G= centre of growity of plane surface
 - P= centre of pressure
 - W = Distance of Centre of pressure brom free surface of Lequid



(a) TOTAL PRESSURE (F) :-

The total pressure on the surface may be determined by obviding the entitie surface into a number of small paratual ships. The force on small staip is then calculated and the total pressure force on the whole area is calculated by interpretting the force on small strop;

Consider a strapp of thickness with and width to at the depth of I know bree contrace of liquid as shown in bigune.

pressure intensity on the strop, p=fgh

Area =5 the steip : dA = bxdh

Total pressure borce on strip, dF = px Area = fgh xb xolh

. Total pressure bonce on the whole surface,

But Soxhxdh= ShxdA

= moment of surface cinea about the breek Surface _ of loquid

- Arrea of surface × Distance of e.y. Grow the bree surface

=AX h

+ F=fgAh

St for woulder the value of P=1000 kg/m3 and g=9.81 m/s2 The force will be in Newton.

(b) Contra of Pressure (h') :-

Centre of pressure is calculated by using the principle of moment, which states that the moment of the resultant bonce about an axis is equal to the sum of moments of the components about the same axis.

"The resultant force F is acting of p, of a distance h' brombre sunface of the lequid as shown in figure. Hence maintent of the borce F about force sunface of the liquid = F xh' -- (1) Moment of force df, acting on a strop about linee sunface of inquid = df xh [: df = fgh x b x dh] = fgh x b x dh xh

Sum of moments of all such burces about free Surface of liquid = offoto fight biddy h = fgfbxthigh

But ShedA = Shedh

= moment of Inertia of the surface about the tree surface of loguld == Io

isum of moments about free surface = fg10 - (2)

where Into moment of Inerative of the anen about an oxer pressing through the city of the anen and powerlies to the tree surface of lequid.

substituting To in equation (3), we get

 $h' = \frac{\mathbf{I}_{4} + \mathbf{h}^{2}}{\mathbf{A} \mathbf{h}} = \frac{\mathbf{I}_{4}}{\mathbf{A} \mathbf{h}} + \mathbf{h} - (4)$

In equilibrith is the destance of city of the origin of the ventical sangues from the surchase of the loguid . Hence from equation (4), it is cleare that

(3) Centre of pressure (i.e. h) the betwee the centre of gravity of the varitient surface.

(2) The distance of centre of pressure been three surface of logural is independent of the density of the logural.

The Moments of Inertia and other Jeometric properdies of Some Important plane surfaces :-

plane Surface	C.G. brom the base	Arren	Moment of Onertici about on nois pour through the and Egg	t goment of inomine about base (ID)
2. Rectangle	x =	bd	6d3 12	<u>63</u> 3
- 16 Triangle A X 19 h	x= <u>h</u> 3	<u>bh</u> 2	<u>bh³</u> 36	<u>643</u> 12

this

Morment of bromant of mendia about an axis passing Inertia about (.67. Area through C.G. and base (16) plane surface briom percalled to base (IG) the Base \$3. Cincle nd4 Rd 2=3 d 67 x 4. Trapezium $9 = (a+b) + (\frac{a^2 + 4ab + b^2}{3b(a+b)} + h^3$ $(\frac{2a+b}{a+b}) = 2^{3} + (\frac{a^2 + 4ab + b^2}{3b(a+b)} + h^3$ G ×

ARCHIMEDES' PRINCIPLE

- of When an object is completely on particulty immensed in a bluid, the bluid exerts an upward board on the object orgunal to the weight of the bluid desplaced by the object.
- I when a solid object is wholly one printly immensed in a blood, the fluid molecules are continuely striking the submerged Surface of the object. The force due to these impacts can be combined into a single bance the buoyant force. The immensed object will be lighter the buoyant force. The immensed object will be lighter to the buoyad up by an amount equal to the weight of the budit it displaces.

BUDYANCY 7

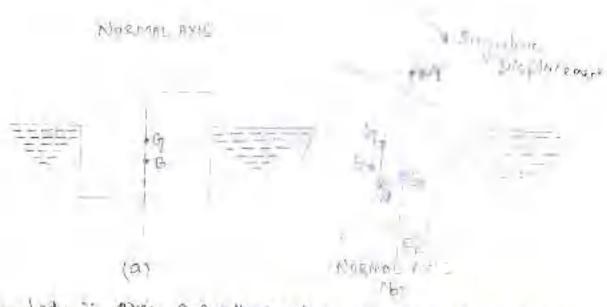
When a body is immensed in a bluid, an upward force is exerted by the fluid on the body. This upward force is equal to the weight of the bluid displaced by the body and is called the force of blueyancy on Simply buoyancy.

CENTRE OF BUDYANCY :-

It is defined as the point, through which the force of buoyancy is supposed to act. As the force of buoyancy is a vertical force and is equal to the weight of the fluid displaced by the body, the Centre of buoyancy will be the centre of gravity. of the fluid displaced.

META-CENTRE :+

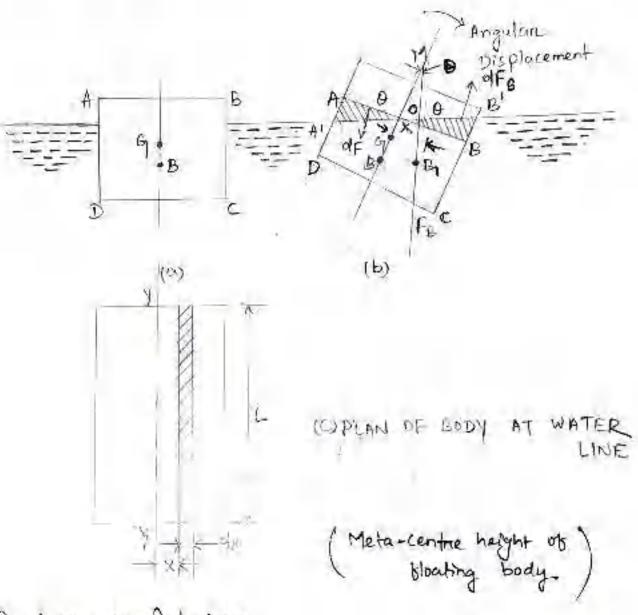
- The is defined as the point about which a body starts , ascellating when the body is filled by a small angle. The meta-culture may also be defined as the point at which the line of action of the force of bourgancy will meet the normal axis of the body when the body is given a small angular alisplacement.
 - -7 Considere a body bloating in a liquid as shown in figure. Let the body is in equilibrium and 'by is the contra of gravity and bits Centre of buoyancy. For equilibrium, both the points lie on the normal axis, which is Nentrical.



Let the body is given a small angular displacement in the clockwise direction as shown in bigune (2). The centre of buoyancy, which is the centre of gravity of the displaced liquid on centre of gravity of the portion of the body sub-menged in liquid well new be shrifted towards night from the normal axis, Let it is at B, as shown in bigune (b). The line of arther of the force of buoyancy in this new position, will intenseet the normal axis of the buoyancy in this new position, will intenseet the normal axis of the buoyancy is some point say M. This point M is called "Meta-centre".

META-CENTRIC HEIGHT &

The distance MSq, i.e. the distance between the meta-centre of a bloating body and the centre of gravity of the body is called meta-centric height.



Couple Due to Wedges :-

Consider towards the right of the axis a small strop of thickness dow at a distance is x from D as shown in bights. The height of strop XX (BOB! = XXO (:: (BOB! = (AOA! = BMB; = 10))

: Anea of steep = Height X Thickness = ax axda 35 L is the length of the bloating body other volume of steep = Anea X L = 2X & X LX da

Similarly, it a small staip of thickness du at a destance on from O to would the left of the axis is considered, the weight of strop un be flynkeidledon. The two weights are ouching in the opposite direction and hence constitute a couple.

Moment of this couple = Weight up Each stapp x Distance between these two weights = fgx OLdx (x+x)

1. Moment of the couple for the whole wedge

Moment of Couple due to shifting of Centre of buoyancy brum B to B, = FB × BB, = FB × BM × Q (= BB, = BM × Q if Q is very = W × BM × Q -(2) (FB = W)

But these two couples are the same thence equating equations (1) \$12), we get

Now Loba = Elemental arrea on the water line shown in figure (c) and = all ... WX BM = 2 fg fat alt

But them figure (c). It is clean that 2 for2 old is the second moment of area of the plan of the body out water. Surface about the axis y-y. Therefore

$$W \times BM = fgE$$
 (where $E = 2 fn2o1A$)
 $\Rightarrow BM = \frac{fgE}{W}$

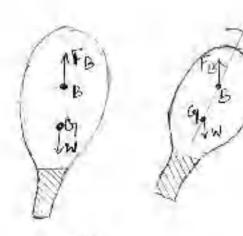
But "W = Weight of the body. = Weight of the bluid displaced by the body = fg x Volume of the bluid displaced by the body = fg x Volume of the body Sub-manged in water = fg x V : BM = $\frac{4}{7} \frac{7}{7} \times \frac{7}{7} = \frac{7}{7} = -\frac{7}{9}$ GM = BM - BG = $\frac{7}{7} - BG$: Metablemtric height = GM = $\frac{1}{7} - BG$ '- (4)

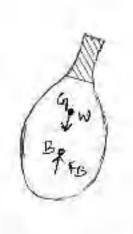
CONDITIONS OF EQUILIBRIUM OF & ELDATING AND SUB-MERGED BODIES

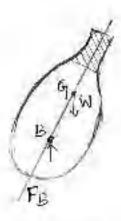
A sub-merged are a floating body is said to be stuble if it comes back to its original position after a slight disturbance. The relative position of the contre of gravity (6) and contre of buoyancy (81) of a body determines the Stability of a sub-merged body.

* Stability of a Sub-manged body :-

The position of centre of gravity and centre of biography in case of a completely submerged body one bixed. Consider a balloon, which is completely submerged in wir. Let the lower porchion of the biography ibralloon centains heavier material. So that its Centre of gravity is lower than its centre of biography as shown in figure (a). Let the weight of the balloon is W. The weight wis eating through by vertically in the downword officertion, while the biograph force Fe is certing vertically up, through B. For the equilibrium of the balloon w= Fg. If the balloon is given an angular clasplacement in the clockwise direction as shown in figure (a); then w and FB kenstoute. A couple acting in the anti-clockwise alized on the position, shown by figure (a) to stable equilibrium.







(4) STABLE EQUILIBRIUM

(b) UNSTABLE

QUILISEDTA

NEVTRAL EQUILIBRIUM

(Stabilities of sub-marged bodies)

(a) stable Equilibrium -

When Wo Fg and point is is above by, the body is said to be it stable equilibrium.

(b) Unstable Equilibrium 1-

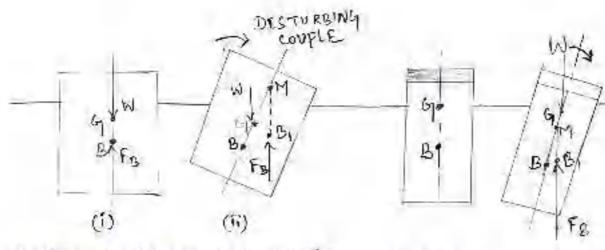
It water the centre of budgancy (B) is below centre of gravity (h), the body is in unstable equilibrium as shown in fig (b). A slight displacement to the budy in the clock wise direction to the body in the clockwise direction, gives the couple due to Ward For also in the clockwise direction. Thus the body does not return to its antigenall possible and been hence the body is in lingtable. equilibrium.

(C) Neutral equilibrium :-

It Fig = W and B and by ane at the same point, as shown in big that, the body is said to be in neutral regulabelium.

+ Stability of Floating Body =>

The stability of a blooking body is determined from the position of Mota-centre (M). In case of bloating body, the weight ob-the body is equal to the weight of loquid displaced.



(a) Stable equilibration M is above 17 (b) Unistable equilibration M is below G.

(Stability of Hoading bodies)

(a) Stable Equilibrium :-

if the point M is above M is above G, the Hoating body will be in stable equilibrium as shown in fig (a). It a slight angular displacement is given to the Hoading body is the

clockwise dimention, the centre of buoyancy shifts from B to B, such that the ventreal line through By earts at on. Then the buoyant bance FB through B, and weight withrough by constitute a couple acting in the anti-clockwise eliteration and thus beinging the floating the floating body in the original position.

(b) Unstable Equilibrium 2-

It the point M is below G1, the bloading body will be in unstable equalibrium as shown in (b). The disturbing Couple is acting in the alcoholic objection. The couple glue to buoyant bonce F3 and w is also acting in the clock wise allower than and thus overcturening the bloating body.

(9) Newtral Equilibrium:

It the point my is dut the centre its greavity of the body the bloating body will be in neutral equilibrium.

CHAPTER-04

TYPES OF FLUID FLOW :-

The fluid flow is classified at 1. (i) Steady and unsteady blows (ii) Uniform and non-uniform blows (iii) Laminar and turbulent blows (iv) Compressible and turbulent blows (v) Compressible and turbulent blows (v) Rotational and turbulent blows and (v) Directup or three domensional blows

(1) Steady and Unsteady blows 7

7 Steady blow is defined as that type of them in which the blood Characteristics like valouty pressure, density etc. at a paint do not change with time. Thue for steady blow, mothermatically, we have

where (xo, yo, zo) is a boxed point in bluid bield

7 Unsteady blow is that type of blow, in which the velocity opressing on density mespect to time, thus mothermatically, for unsteady-bloc

(1) Uniform and Non-Uniform Front of these of these in which the is defined as that type of these in which the velocity at any given time does not change with respect to space the length of division of the trave). Mostly matically, box uniform the (2) += constant = 0 where on = change of velocity

Ds = Length of blow in the direction s

+> Non-Uniborion Blow is that type of blow in which the velocity at-any given time Changes with respect to space. Thus, mathematically, box non-uniform blow

(Ds) to constant = D

(iii) Laminan and Turbulent Flow 7

- -7 Laminar blow is defined as that type of blow in which the blowd landocles more along well-defined paths on stream line and all the steam. linescare strewight and parcallel. Thus the parcticles more in laminas on layers. gliding smoothly over the adjacent loyer. This type of blow is also called steam-line blow on viscous blow.
- •> Turbulent blow is that type of blow in which the field parabitles move is a zig-zay way. Due to the movement of blowd parabitles on a zig-zay way, the eddres formation takes place which are responsible for high energy loss for a pipe blow, the type of blow is determined by a non-dimensional number. Called the Reynold number.

where D = Docimeters of pipe

V = mean velocity of blow in pipe

V = Kinematic Viscocity of Bluid

and 36 the Reynold number is less than 2000, the flow is called laminar, 35 the Reylond number is more than 4000, then it is called turbulant blow. 35 the Reynold number lies between 2000 and 4000, the blow may be laminar on turbulant.

(Compressible and Pricompressible Flows ?

The bluid changes brown point to point on in other words the density of the bluid changes brown point to point on in other words the density of it not constant box the bluid. Thus, mathematically, fore of Compressible flow,

of \$ constant

-Dicompressible blow is that type of blow in which the density is constant bouthe blow blow. Liquids are generally incompressible cohele gases are compressible. Mathematically, box & incompressible blow; P=constant

(V) Rotational and Introtational Flows =>

Rotectional blow is that type of blow in which the bluid panticles while blowing along steam times, also rectedee about their two axis. And it the bluid powericles while blowing along steam lines, do not net one obset their own axis then that type of blow is called innertational blows

Vi) One-, Two-, and Three-Dimensional Flows :-

"The dimensional bloco is that type of bloco in which the blow parameter such as velocity is a transform of time and one space ap-ordinate only say at. For a steady one domentional blow, the velocity is a bunction of one space. Co-ordinate only. The variation of velocities in other two mutually perpendicular direction is als used negligible. Hence, mothematically, for one-dimensional blow,

u=\$(a), v=0 and w=0

when u, v. and w are velocity components in x, y and z directions mespectively, -7 Two-domansional blow is that type of blow in which the velocity is a tondo bunction of time and two rectangular space co-ordonates only come say a and y. For a steady twodimensional blow the velocity is a function of two-space co-oridinate only. The veloc variation of velocity in the third direction is negligible. This + mathematically for two-dimensional blow,

-1 Three-domensional blow is that type of blow in which the velocity is a bunction of time and three mutually perpendicular directions. But bor a steady three-domensional blow the blowd parameters are bunctions of three space co-ordinates (ne, y and Z) only - Thus, mathe matically, box three domensional stow " u= \$1(21, y, 2), N= b2(2, y, 2), and W= 59(24, y, 2)

RATE OF FLOW OR DISCHARGE (Q)

It is defined as the quantity of a fluid blowing per second through a section of a pipe or a channel. For an incompressible blurd (on locuid) the mode of blow on dischange is expressed as the volume of bland bloging econors the section per second. For compressible bluids the mate of blow is usually expressed as the weight of bluid blowing actions the section. Thus Ofor loquids the Units of Qane m3/s on litris/s (iii) Fore gases the write of Q is kg 5 /s on Newton/s Consider a logued blowing through a pipe in which

A = Crucks-sectional area of pipe

V= Average velocity of bland eccross the section

CON CON Then Discharge Q = AXV.

CONTINUITY EQUATION 7

The equation based on the principle of Conservation of mass is called Confinuity equation. That box a bland blowing through the pope of all the cross-section, the quantity of blued per second is constant. Consider two enous sections of a pipe as shown in biguese; let V = Average velocity at Cross-section 1-1 -Pr = Density at section 1-1 AF= Arran of Pope at section 1-1 and V21 f21 Az ane connesponding value at section 2-2, Then note of thow ent section 1-1= P. A.V. Rote of Stow out section \$2-2 = P2A2V2 Direction of thow fanny anna many anny According to low of Conservation of TRASH. (Fluid blowing through a pipe Rode of blow at section 1-1 = Rade of blow out section 2-2 On Annual I PiAIVI = P2A2V2

The above equation is pupplocable to the compressible as well as incompressible bluds and is called Continuity Equation. .

then $f_1 = f_2$ and continuity requestion revoluces to $\left[A_1V_1 = A_2V_2\right]$

EQUATIONIS OF MOTION =>

According to Newton's second low of motion. The net force Fre acting on a bluid element in the clinection of a is equal to make in of the bluid element multiplied by the acceleration. And in the 2-direction.

Thus mathematically; Fox = m.a.u.

In the blund blow, the following bonces are present,

(1) Fg, gravity boace

(ii) fp, the pressure bonce

(10) FV, bonce due to Viscosity

(in Ft, porce due to turbulence

(1) Fc, bonce due to compressibility

Thus in equation, the net board

Fx = (Fq) a + (Fr) a + (Fr) at (Fc) at (Fc) at

() It the fonce due to compressibility, the is negligible, the nesulting net fonce

Fx = (Eg)he+(FDat(Ev)at(G)a

and equation of midning area called Reynold's equations.

(i) For Elow, where (Ft) is negwyible, the negwood equation resulting equations of motion one known as Navier-stokes Equation.

(19) It the blow is assumed to be ideal, Viscous bonce (Fv) is zero and equation of motions are known as Euleris equation of mation.

EULER'S EQUATION OF MOTION 7

This is equation of motion in which the back there is gravity and pressure are taken into consideration. This is deceived by consideration the motion of a blust element along a stream line as :

consider a stream-line in which blow is taking place in a direction as shown in bigune. Consider a cylindrical element of cross-section dd and length dis. The borce acting on the cylindrical element are

1. pressure bence pd A in the above the of 5100

2. Pressure borce (p+ 3p ds) de opposte to the direction of the. 3. Weight of element pgolads.

let 0 is the angle between the objection of blow and the line of action of the weight of element.

The resultant torse on the bluid element in the direction of os must be equal to the mass of thuid element X acceleration in the

direction s. : pdA-(P+ de ds) dA- fgd Adps. Los 0 = fdAdsXas where as is the neceleration m the otherestion of S. Now, as = dv, where V is a transform of s and +. ds/e d= = 양성 + 행사 = var + ar (: ar = v) (6) to the films is structly, Fjalads (10) av =D forces on a blund element

$$\therefore C(s = \frac{VdN}{ds})$$

Substituting the value of as in syn () and simplifying the equiviliant, 10,0 get - OP alsola - Pg dads costo - pdads & de Dividing by fdedA; -- dp -g cos 0 = Valu on de + geos o + v gs =0 But brom big(b), Loo have cos of and as · + gras + gras + volv = 0 on gr gaz + gaz + valv = 0 de+gaz+van=0 .--(2) Equation (2) is known as Eulen's equation of motion. BERNOULLI'S EQUATION FROM EULER'S EQUATION 7 Bennoulli's equation is obtained by integrating the Euler's equation of motion dis Jdp + Sgotz + Svolv = constant It blow is in compressible, f is constant and $\frac{1}{p}$ +gzt $\frac{N^2}{2}$ = constant >> P+ + 2g + Z= Bonstant Equation (3) is a Berchoulli's equation in which, To = pressure energy per unit weight of third on pressure $\sqrt{2}/2g = kinetic energy per unit weight on kinetic head$ Z = potential energy per unit weight on potential head

ASSUMPTIONS 2-

- The following are the assumptions made in the derivation of Bernoulli's equation:
 - Withe bluid is idealine. Viceosity is zero.
- (1) The blow is steady.
- (iii) The klow is in compressible.
- (19) The Blow is Increatedional.

PRACTICAL APPLICATIONS OF BERNOULLI'S EQUATION --

Bernoullis equation is applied in all problems of incompressible Hund blow where energy considerations are involved. But we shall consider its application to the bollowing measuring devoces:

- 1. Venturimeter
- 2. Onlittle meter
- 3. Pitot-tube

(1) Venturimeter =7

- A Venturie meter is a clevice lised box measuring the made of a time of a time of a time of a time of three parts:
 (1) A short converging part,
 (2) Threat and (iii) Diverging part.
- I to bis based on the principle of Bornow 10's equation.

Expression for mate of blow through Venturimeter 2-Consider a venturitmeter billed m a horizontal pipe through which a blued is thowing (say weiter), as shown in begure. THROAT INLET Let Pi = pressure at section (1) [VENTURIMETER] of - diameters of inlet on at cochion (1), NI= velocity of bluid on section (1), a = Anen at soction(1) = A di? and dz, Pzivziaz are concresponding values of section (2); Applying Bennoullo's equation and section (1) and (2), we get $\frac{P_1}{P_3} + \frac{v_1^2}{89} + z_1 - \frac{P_2}{P_3} + \frac{v_2^2}{29} + z_2$ As pipe is horizontal, hence = Z1=Z2 : $\frac{P_1}{P_3} + \frac{V_1^2}{2g} = \frac{P_2}{P_3} + \frac{V_1^2}{2g} \text{ pn } \frac{P_1 - P_2}{P_3} = \frac{V_1^2}{2g} - \frac{V_1^2}{2g}$ But Pi-Pz is the difference of pressure heads at sections land 2 and it is equal to hor PI-12 = h Substituting this value of <u>PiPz</u> in the above equation, we get $h = \frac{V_1^2}{29} - \frac{V_1^2}{29}$

Now applying continuity equation at section 182

$$a_1 v_1 = a_2 v_2 \quad \text{or} \quad v_1 = \frac{a_2 v_2}{a_1}$$

Substituting the value of V, in equation (5),

$$\begin{split} h &= \frac{v_{2}^{2}}{2g} = \frac{\left(\frac{a_{2}v_{2}}{a_{1}}\right)^{2}}{2g} \\ &= \frac{v_{2}^{2}}{2g} = \left(1 - \frac{a_{2}^{2}}{a_{1}^{2}}\right)^{2} = \frac{v_{2}^{2}}{2g} \left(\frac{a_{1}^{2} - a_{2}^{2}}{a_{1}^{2}}\right) \\ &= \frac{v_{2}^{2}}{2g} \left(1 - \frac{a_{2}^{2}}{a_{1}^{2}}\right)^{2} = \frac{v_{2}^{2}}{2g} \left(\frac{a_{1}^{2} - a_{2}^{2}}{a_{1}^{2}}\right) \\ &\to v_{2}^{2} = 2gh \frac{a_{1}^{2}}{a_{1}^{2} - a_{2}^{2}} = \frac{a_{1}}{a_{1}^{2} - a_{2}^{2}} \\ &\Rightarrow v_{2}^{2} = \sqrt{2gh} \frac{a_{1}^{2}}{a_{1}^{2} - a_{2}^{2}} = \frac{a_{1}}{a_{1}^{2} - a_{2}^{2}} \sqrt{2gh} \end{split}$$

Discharge, Q=azV2

=?
$$Q = \frac{a_1 a_2}{\sqrt{a_1^2 - a_2^2}} \times \sqrt{2gh} = -(6)$$

Equation(6) gives the discharge under ideal conditions and is called theoretical discharge. Actual discharge will be less than theoretical discharge.

where Cole Co. estimated of Vontainimeter and its value is less. than 1. (Co-estimated of discharge)

Value of the givenby different 12-tube manometers.

Case-1: Let the distremential manumeters contains a liquid which is

heavier than the logicity blowing through the pipe.
Let
$$S_h = Specific growity of the heavier liquid $S_0 = Specific growity of the liquid flowing through pipe $N = Oper Difference of the heavier liquid column in U-tubesthen $h = N \left[\frac{S_h}{e} - 1 \right]$$$$$

Case-II: 24 the differential manomater tentions aloud which is
lighter than the liquid blowing through the pipe, the value of
h is given by:

$$h = \propto \left[1 - \frac{2}{50}\right]$$

Se = specific gravity of basis-lighter liquid in U-tube
So = specific gravity of block blowing through pipe
 $\pi = D$ interence of the lighter liquid columns in U-tube.
ISC m respectively, find the doctories through the pipe, is the
velocity of wooder fielding through the pipe at section 1 is 2 and to cm R
TSC m respectively. Find the doctories through the pipe, is the
velocity of wooder fielding through the pipe at section 2.
This case is the velocity of section 2.
 $M = 500 \text{ (m}, d_2 = 15 \text{ (m} = 2.15 \text{ m})$
 $M = 500 \text{ (m}, d_2 = 15 \text{ (m} = 2.15 \text{ m})$
 $M = 500 \text{ (m}, d_2 = 15 \text{ (m} = 2.15 \text{ m})$
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 $M = 500 \text{ (m}, d_2 = 100 \text{ m} = 2.15 \text{ m})$
 $M = 0.0001 \text{ x S}$
 $= 3.092 \text{ (m}, d_2 = 100 \text{ (m} = 2.15 \text{ m})$
 $= 0.00392 \text{ m}) \text{ (S}$
 $M = 0.0001 \text{ x S}$
 $= 3.092 \text{ m}) \text{ (S}$
 $M = 0.00392 \text{ m}) \text{ (M} = 2.294 \text{ (M} m)$

= 2-24 (Ang)

$$d_{1} = 30 \text{ Given} = 0.20 \text{ m}$$
$$d_{2} = 30 \text{ Given} = 0.20 \text{ m}$$
$$d_{3} = 15 \text{ Gm} = 0.15 \text{ m}$$
$$d_{3} = 15 \text{ Gm/s} = 0.15 \text{ m}$$
$$d_{3} = 3.5 \text{ m/s} = 0.15 \text{ m}$$
$$d_{3} = 2.7 \text{ m/s} = 0.15 \text{ m}$$

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$$Q_{1} = A_{1} \times V_{1}$$

$$= \frac{\pi}{4} A_{1}^{2} \times V_{1}$$

$$= \frac{\pi}{4} \times (e \cdot 30)^{2} \times 245$$

$$= \frac{\pi}{4} \times 0.09 \times 245 = \frac{3441}{4} \times 0.09 \times 2.5$$

$$= 0.78 \times 0.09 \times 2.5$$

$$= 0.176 \text{ mP}/5$$

In tigune,

-7 V3 - 0.1196 > V3 = 6.4 m/s (Ans)

on, $Q_1 = Q_2 + Q_2$ = $A_1 V_1 = A_2 V_2 + A_3 V_3$ の町は2×1 = 子×はシメン2+子×は2×2 -> 7 [(0.30) ×2.5] = # 2 (0.20) × 2 + (0.15) × × V3] 4. -> (30×10-2)2×25 = (20×10-2)2×3+(15×10-2)2×V3 7(30)2×215=(20)2×2+(15)2×V3 =) 900 × 2.5 = 400 × 2 + 8225 × 3 = 2250 = 800 + 225 Vs A 11 148 => 2250-800 = 225 V3 11⁹ - 1 - 2

The a thirty of the the of the

Não 3 m/s L Re- 2 Rao

te mys

(3) Water blows through a pipe AB 1.2 m. in drameter. Velocity of 3mls through a pipe. BC 1.5 mm drameter. At C the pipe branches, Branch CD 0.8 m. moliameter and Carended 1/3 of the the tow in AB. The relocity on the " break CE is Ris m/s. Find the discharge and MB, velocity in BC, velocity on CD and the drameter of CE? D 1.5 m & 0.8 m)) 1.5 m @ 0.8 m)) Quit 30.05 C. 0 1-30.05 U-2.5 MUS GANEN, A 1.2m B

01AB 2, 1.2 m $d_{BC} = 1.5 m$ dep = D.8m de= ??

$$V_{AB} = 3m/s \qquad Q_{AB} = ?$$

$$V_{BE} = ? \qquad Q_{EC} = ?$$

$$V_{CD} = ? \qquad Q_{CD} = \frac{1}{3}Q_{AB}$$

$$V_{CE} = 25m/s \qquad Q_{LE} = \frac{2}{3}Q_{AB}$$

Rate of discharge at AB,

$$Q_{AB} = A_{AB} \times V_{AB}$$

= $\frac{T}{7} (D_{AB})^2 \times V_{AB}$
= $\frac{T}{7} (D_{AB})^2 \times V_{AB}$
= $\frac{T}{7} (D_{AB})^2 \times 3' = \frac{T}{7} \times 1.444 \times 3 = 0.76 \times 3 \times 1.444$
= $\frac{T}{7} (1.2)^2 \times 3' = \frac{T}{7} \times 1.444 \times 3 = 0.76 \times 3 \times 1.444$
= $3.39 \text{ m}^3/5$

From bigune, are then

$$Q_{AB} = Q_{GC}$$

 $\Rightarrow A_{AD} \times V_{AB} = A_{BL} \times V_{BC}$
 $\Rightarrow T (e1_{AD})^2 \times 3 = T \times (d_{BC})^2 \times V_{BC}$
 $\Rightarrow T (e1_{AD})^2 \times 3 = T \times (d_{BC})^2 \times V_{BC}$
 $\Rightarrow T (e1_{AD})^2 \times 3 = T \times (d_{BC})^2 \times V_{BC}$
 $\Rightarrow 3.3q = 1.76 \times V_{BC}$
 $\Rightarrow 3.3q = 1.76 \times V_{BC}$
 $\Rightarrow V_{BC} = \frac{3.39}{1.76} = 1.92 \text{ m/S}$
 $\therefore \text{ velocity in } BC \text{ is } (-92 \text{ m/S})$
 $\therefore \text{ velocity in } BC \text{ is } (-92 \text{ m/S})$
Then, $Q_{ED} = \frac{3}{3}Q_{BD} = \frac{1}{3}\times 3.39 = 1.131 \text{ m/S}$
 $Q_{CE} = Q_{AB} - Q_{CD} = 3.3q - 1.131 = 2.252 \text{ m/S}$
 $PT (Q_{CE} = \frac{2}{3}Q_{AB} = \frac{5}{3}\times 3.3q = 2.252 \text{ m/S}$
 $Velocity Tr CD + (1.131 = 2.252 \text{ m/S})$
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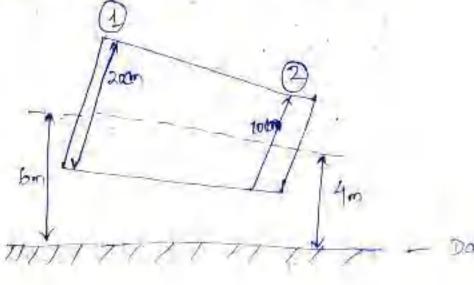
 $= \frac{1}{2} N_{CD} = 2.25 \text{ m/s}$ $= \frac{1}{2} N_{CD} = 2.25 \text{ m/s}$ $= \frac{1}{2} N_{CD} = 15 \quad 2.25 \text{ m/s}$ $= \frac{1}{2} N_{CE} \text{ can get brown this expression,}$ $= \frac{1}{2} N_{CE} = \frac{1}{2} N_{CE} \text{ censes}$ $= \frac{1}{2} N_{CE} = \frac{1}{2} N_{CE} \text{ consession}$ $= \frac{1}{2} N_{CE} = \frac{1}{2} N_{CE} \text{ consession}$

 $r(dec)^2 = 1.963$ $r(dec)^2 = 1.152$ $r(dec)^2 = \sqrt{1.152}$ $= 1.073 m_1$

- diameter of CE is 1.073 m. (Ang)

D Water is blowing through a pipe having diameter 20 cm. & 10 cm at section 122 nespectively. The node of thow through pipe is as litrefsee. The section 1 is 6 m. above the datum and section 35 litrefsee. The section 1 is 6 m. above the datum and section 1 2 is 4 m. above the datum. If the pressure at cross section 1 is 39.24 Non- then bind out the Intensity of pressure at section 2

(me)



Datum line

Given,

$$d_{1} = 20 \text{ cm}, = 0.10 \text{ m} \quad Z_{1} = 6 \text{ m}.$$

$$d_{2} = 10 \text{ Cm}, = 0.10 \text{ m} \quad Z_{2} = 4 \text{ m}.$$

$$(Q = 36.91 \text{ s}) \quad (q = 9.81)$$

$$R = 36.91 \text{ s} \quad (q = 9.81)$$

$$R = 36.91 \text{ s} \quad (q = 9.81)$$

$$R = 36.91 \text{ s} \quad (q = 9.81)$$

$$R = 36.92 \text{ s} \text{ s}$$

......

=> 1/2 = +1.075 × 9810 = 402945.75 N/m2-= 40,29 N/cm2 (Ans)

(3) An oil of specific gravity ors is blowing through a . Verturismeter having in let diameter 20 cm. and throughtdrameter 10 cm. The oil Americany distancential manometers drameter 10 cm. The oil Americany distance the discharge of shows a reading of 25 cm. Calculate the discharge of oil through horizontal venturimeter taking Cd = 0.98 ?

(ms) Given, $d_1 = 20 \text{ Cm} = 0.20 \text{ m}$ $d_2 = 10 \text{ Cm} = 0.10 \text{ m}$ $S_{ne} = \text{specific gravity of oil = 0.8}$ $S_h = \text{specific gravity of mencuny = 13.6}$ $n_{=}: \text{Distensional reading = 25 cm} = 0.25 \text{ m}$

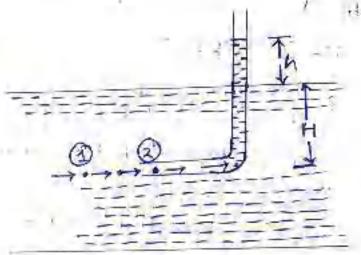
According to case - I,

$$h = \pi \left[\frac{s_{h}}{s_{a}} - 1 \right]$$

= 0.25 x $\left[\frac{13.6}{0.8} - 1 \right] = 0.25 \times (17 - 1) = 0.25 \times 16$
= 4 m = 4000 cm

Pitot-Tube 7

It is a device used for measuring the velocity of blow at any point in a pipe on a channel + It is based on the principle that if the velocity of this at a point becomes zero, the pressure there is increased due to the conversion of the kinetic energy into pressure energy. In its simplest form, the pitot-tube consists of a glass tube, bent at rought angles as shown in bigure.



Pitot - tube

The lower end, which is bent through 90° is directed in the up steam direction as shown in figure. The loguid rises up in the tube due to the Conversion of kinetic energy into pressure energy. The velocity is determined by measuring the rise of liquid in the tube.

Consider two points (1) and (2) at the same level in such a way that point (2) is just as the inlet of the pitot-tube and point (1) is bar away know the tube.

Let
$$P_1 = intensity of pressure at point (1)$$

 $M_1 = velocity of flow at (1)$
 $P_2 = Pressure at point (2)$
 $V_2 = velocity out point (2), which is Zero
 $V_2 = velocity out point (2), which is Zero
 $H = elepth of tube in the loguid
 $H = rise of loguid in the tube cubove the free surface$$$$

Applying Bernouli's equation at points (1) and (2), we get

$$\frac{P_1}{P_2} + \frac{\sqrt{2}}{2g} + \tilde{z}_1 = \frac{P_2}{P_3} + \frac{\sqrt{2}}{2g} + \overline{z}_2$$
But $T_1 = Z_2$ as points (3) and (3) are on the same line and $V_2 = 0$

$$\frac{P_1}{P_3} = \text{pressure head at (2)} = H$$

$$\frac{P_2}{P_3} = \text{pressure head at (2)} = (h + H)$$
Substituting these values, we get

$$H + \frac{\sqrt{2}}{2g} = (h + H)$$

$$H + \frac{\sqrt{2}}{2g} = (h + H)$$
This is theoretical invelocity. Arctual velocity is given by
(N) act = C_V Z_g h
where $C_V = C_0$ - ethicient of pitot-tube.

$$V = C_V Z_g h$$

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SCHAPTER -053 ORIFICE

Introduction ?

Onlibice is a small opening of any creases section (curp as circular triangular , rectangular etc.) on the side on at the bollom of a tank, through which a blund is blowing. A mouth piece is a short length of a pape which is two acto three times its deameters in length, kotted in a tank on vessel containing the bluid. Droffices as well as mowth preces are used for measuring the rode of flow + of bluid,

F.MS

Classification of Dreibices >

The onliging ane classified on the basis of their size, shape, nature of discharge and shape of the upsteam edge. The following

are the important classifications :-(1) The onthices are classified as small on the or large orifice depending upon the size of profile and head of liquid from the Centre of the onlyfice. It the head of liquid know the centre of omigice is more than five times the depth of oragice, the origine is called small onitfice. And it the head of liquide is less thanking times the depth of dreffice off is known as large endfice. a) the orafices are classified as (i) Cinculan orafice,

(1) Tretangular onthere (11) Roctangular mitice and

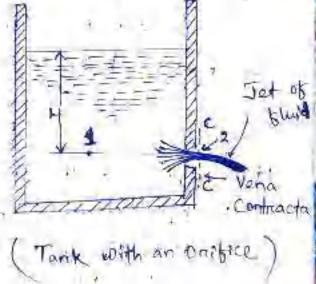
in square onabice depending upon their chase-sectional anexis 2) The prefices are clossified as (1) sharp-edged onibice and a (1) Fiell-mouthed ontifice depending upon the shape of cipitar in Rely of the origins.

(4) The Onlysces are classified as

- (7) Firs dischanging onibices and (1) Inscined on sub-menged probles depending upon the noture of discharges.
- The submanighed onlifices and the paneliality submanighed onlifices.

Flow through an Onifice of Consider a tank bitted with a circular profice in one of its sides as shown in figure.

Let the the head of the liquid above the confre of the antibice. The liquid blowing through the origine borns a set of liquid whose area of cross-section is less than that of onifice. The area of let of bluid goes on decreasing and at a section C-C, the area is minimum. This section is appreximately at a distance of half of diameter of the onifice. At this section the streamlines are straight and parallel to each other and perpendicular to the plane of the onifice. This section is called "Vence-Contracte". Beyond this section the set diverges and is distanced in the Beyond this section by the gravity. Built direction by the gravity. B



But $\frac{P_1}{P_2} + \frac{v_1^2}{2g} + Z_1 = \frac{P_2}{P_2} + \frac{v_2^2}{2g} + Z_2$

But 7,= 72.

 $\frac{P_1}{P_3} + \frac{V_1^2}{2g} = \frac{P_2}{P_3} + \frac{V_2^2}{2g}$

Now $\frac{P_1}{P_2} = H$ $\frac{P_2}{P_2} = O \left(\text{cotmospherede pressure} \right)$

Vi is very small in comparison to ve as area of tank is very lange as compared to the area of the Jet of liquid.

$$H + 0 = 0 + \frac{V_2^2}{2g}$$

 $V_2 = \sqrt{2gH}$

This is theoretical velocity. Actual velocity will be less than this value.

- The hydromlic co- efficients one :-'I Co-abbicient of velocity, C/ 2] Co-efficient of Contraction, Ce 3] Co-efficient of discharge, Cd
- (4) Co-effectiont of Velocity (CV):->

It is defined as the notion between the actual velocity of a Jet of liquid at vena-contracta and the theorietical of Jet. It is denoted by Excand mathematically inclusing given as $C_V = \frac{Actual}{Velocity}$ of jet at venar contracta Theoretical velocity = VagH , where V= actual velocity, VagH = Theoretical velocity

The value of Cy varioes briom 0.95 to orgin for different. onifices, depending on the shape, size of the Oriflice and on the head under which blow takes place.

Generally, the value of Cr=0.98 is taken for sharp-redged prifices.

(2) Co-efficient of Contraction (Cc):-

It is defined as the natio of the area of the jet at Vena - Contracta to the arrea of the briffice. It is denoted by Gc.

Let a = area of britfice and ac = area of Jet at Vega-Contralta C'= anea of det at vena-Contracta anea of Draffice

The value of Cc varies from Diby to visig depending of shape. and size of the problec and head of liquid under which flow takes place in generical the value of Co may be taken as Diby.

(3) Co-efficient of Discharge (Cd):-

It is defined as the notio of the actual discharge broom an orcifice to the theoretical discharge from the orcifice. It is denoted by Cd. 25 Q is actual deschange and Qth is the theoriefical discharge then mathematically, Cd is given be Col = @ = Actual Velocity X Actual Area Theoretical velocity X Theoretical area - Actual Velocity X Actual Area Theoretical velocity Theoretical area

Cd = CvxCc

The value of Col variates from 0.61 to 0.65. For general purpose the volue, of Col it today as 0.62.

NOTCH

Introduction

A notch is a device used for measuring the rade of flow of a Would through a small channel on a tank. It may be defined as a opening in the side of a torrik or a small channel in such a really that the transforme in the tank on channel is below the top edge of the opening.

A wear is a concrete on masonary structure, placed in an open channel over which the flow occurch. It is generally in the form of verdical wall, with a sharp edge out the top, munning all the way across the open channel. The notch is of food! soze whole the wear is of a bagger size. The notch is generally made of metallic plates while weir is made of Concrete or masonary structure.

1. Nappe on vein :- The sheet of water throwing through a notch 2 Creet on Still on the bottom edge of a notch on a top of a weie over which the bottom the booter flows, is known as the Sill see on Crest.

Elassification of Notes and weites ?

The notches are classified as : (1) According to the shape of the opening: (2) Rectangular notch (b) Tricingular notch (c) Trapozoidal notch and-(d) Stepped notch

(2) According to the effect of the sides on the happe: (a) Notch with end contraction

(b) Notch without and contraction on suppressed notch Weine one classified according to the shape of the opening, the shape of the Creat, the effect of the side on the nappe and nature of discharge. The following are important classification.

(a) According to the shrupe of the opening :

(1) Rectangular wein (11) Triangular wein and (11) Trapezoidal wein (Cippollell+1 wein)

(b) According to the shape of the crest :-

(1) Sharp-Englied web.

(1) Broad-Crested weir

(11) Mannow-Crested wein and

UN Deper-Shaped, weite,

(c) According to the effect on sides on the emerging happe; (c) Weire with end contraction and () Weire without end "Confre action

Discharge over a Reetingular Notch on Weire The expression for descharge over a rectangular motion or were is the same. Nappe Nappe H h Cnest * Crest on A (a) Rectangular (c) section at Notch (b) Rectangular, wela . . . Crest (Rectangulare notch and weire) Consider a rectangular notch on wein provided in a channel Carrying water as shown in figure. Lef M= Head of Water over the criest L= Length of the noteh on wein ton finding the discharge of water flowing over the wein on noth. Consider an elementary horizontal cetrip of wader of thickness dh and length L at depth h from the free & surface of wader is Shown in frigues. The area of ship = Lxdh and theoretical velocity of water blowing through stapp = vagh The discharge da, through strip is de = Col x Anna of strop x Theoretical Velocity = Col x. Lx dh x vagh where Gd = co-etoscient of abschange

The total discharge, (R, box the whole notch on weire is deformined by integrating equation (3) between the limits 'O and H.

$$P_{A} = \int_{0}^{H} C_{A} \cdot L \cdot \sqrt{2g} \int_{0}^{H} h^{1/2} dh$$

$$= C_{A} \times L \times \sqrt{2g} \int_{0}^{H} h^{1/2} dh$$

$$= C_{A} \times L \times \sqrt{2g} \int_{0}^{H} \frac{h^{3/2}}{2} \int_{0}^{H}$$

$$= C_{A} \times L \times \sqrt{2g} \int_{0}^{L} \frac{h^{3/2}}{2} \int_{0}^{H}$$

$$= C_{A} \times L \times \sqrt{2g} \int_{0}^{L} \frac{h^{3/2}}{2} \int_{0}^{H}$$

$$= C_{A} \times L \times \sqrt{2g} \int_{0}^{L} \frac{h^{3/2}}{2/2} \int_{0}^{H}$$

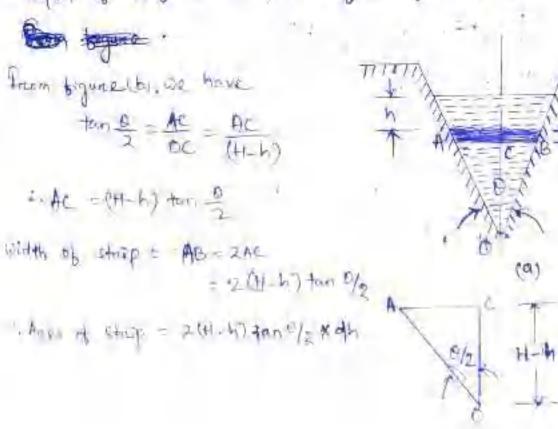
Dischange Over a Triangular Notch or Weire of

The expression for the discharge over a trivingular notten or well is the same. It is the derived as :

Let H = head of water above the V-notch O= angle of notch .

Consider a honoroundal strop of boater of thrances did at a depth of h from the bree, surface of water as shown in bigune.

11/11



The theoretical velocity of where through strop =
$$\sqrt{2gh}$$

= Discharge, through the strop,
 $dq = c_{qx}$ Area of strop x velocity (theoretical)
 $= c_{dx} a(H-h) tan 9/2 x dh x Vagh$
 $= 2c_{d} a(H-h) tan 9/2 x dagh x dh$
= $2c_{d} a(H-h) tan 9/2 x Vagh x dh$
= $2c_{d} x tan 9/2 x Vag (H(H-h) h Va dh)$
 $= 2c_{d} x tan 9/2 x Vag (HhhV2 - h)/2) dth$
 $= 2xc_{d} x tan 9/2 x Vag (HhhV2 - h)/2) dth$
 $= 2xc_{d} x tan 9/2 x Vag (HhV2 - h)/2) dth$
 $= 2xc_{d} x tan 9/2 x Vag (HhV2 - h)/2) dth$
 $= 2xc_{d} x tan 9/2 x Vag (HhV2 - h)/2) dth$
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 $= 2xc_{d} x tan 9/2 x Vag (HhV2 - h)/2) dth$
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 $= 2xc_{d} x tan 9/2 x Vag (HhV2 - h)/2) dth$
 $= 2xc_{d} x tan 9/2 x Vag (HhV2 - h)/2) dth$
 $= 2xc_{d} x tan 9/2 x Vag (HhV2 - h)/2) dth$
 $= 2xc_{d} x tan 9/2 x Vag (HhV2 - h)/2) dth$
 $= 2xc_{d} x tan 9/2 x Vag (HhV2 - h)/2 - \frac{3}{5} H^{5/2}]$
 $= 2x c_{d} x tan 9/2 x Vag (HhV2 - h)/2 = 1$
Discharge, $Q = \frac{8}{15} x 0.6 x 1 x Vax 9.6 x H^{5/2} = 1.417 H^{5/2}$

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T.M?

LIDSS DY Energy In popes of

When a bluid the blowing through a pipe, the bluidt expensionces some respirance due to which some of the energy of bluid is lost. This loss of energy is classified as:

Energy losses 1 t 1 1 1 2. Minor Energy losses 1. Major Energy losses This is alle to this is due to brickion (a) Sudden expansion and 77 is calculated · of ppeby the following (b) Sudden Contraction foremulae: of pipe 11 (a) Dancy - weis bach formula (c) Bend in pipe (b) Chezys: formula . wh pipe bittings etc. (e) An obstantion in pipe

LOSS OF Energy (OR, HEAD) DUE TO FRICTION +

14) Dancy - Wess bach Formulas-

The loss of head (on energy) in purpose pipes due to furction is calculated brom Dancy-weisbach equation which has been derived in chapter to and is given by

$$h_{b} = \frac{4.5.L.V^{2}}{dx_{2}g}$$
 (1)

where he = loss ob head due to brickion ,

Reyrolds number

= 16 for Re X 2000 (Viscous blow)

$$= \frac{0.079}{R_{2}^{1/4}} \text{ for } Re Varying from 4000 to 10^{6}$$

$$L = \text{ length of pipe}$$

$$V = \text{ mean velocity of blow}$$

$$d = \text{ objective of pipe},$$
(b) Cherzy's Foremula for loss of head due to kniction in pipes...
Refer to Chapter to arcticle to in which expression bon loss of head due to briction in pepe pipes is derived.
Equation (iii) ob eachede to us

$$h_{b} = \frac{5}{P_{3}} \times \frac{P}{P} \times L \times V^{2} \qquad (2)$$
where $h_{b} = \text{loss of head due to briction}$

$$P = \text{ watted perimeter of Pipe}$$

$$L = \text{ length of Pipe}$$

$$V = \text{ inean velocity of blow}$$
and the reation of $\frac{A}{P} \left(\frac{Anea of blow}{Parameter[welth]} \right)$ is called hydrowly
mean depth on hydrowlic readous and rs' denoted by m.

$$\frac{1}{161} \text{ win x h_{b}} = \frac{1}{P_{3}} \times L \times V^{2} + \frac{1}{161} \text{ or } X + \frac{1}{P_{3}} \times \frac{1}{X} \times \frac{1}{X}$$

$$\frac{1}{161} \times 1 \times V^{2} \times \frac{1}{161} \text{ or } X + \frac{1}{161} \times 1 \times V^{2} \times \frac{1}{161} \text{ or } X + \frac{1}{161} \times 1 \times V^{2} \times \frac{1}{161} \text{ or } X + \frac{1}{161} \times 1 \times V^{2} \times \frac{1}{161} \text{ or } X + \frac{1}{161} \times 1 \times V^{2} \times \frac{1}{161} \text{ or } X + \frac{1}{161} \times 1 \times V^{2} \times \frac{1}{161} \text{ or } X + \frac{1}{161} \times 1 \times V^{2} \times \frac{1}{161} \text{ or } X + \frac{1}{161} \times 1 \times V^{2} \times \frac{1}{161} \text{ or } X + \frac{1}{161} \times 1 \times V^{2} \times \frac{1}{161} \text{ or } X + \frac{1}{161} \times 1 \times V^{2} \times \frac{1}{161} \text{ or } X + \frac{1}{161} \times 1 \times \frac{1}{$$

Let $\sqrt{\frac{1}{5}} = C$, where C is a constant known as Chezy's Constant and $\frac{h_5}{L} = \tilde{c}$, where \tilde{c} is loss ob should per unit length of pope substituting the values of VP3 and the in equation = (3) we get , V = CVmi : - (4).

requedion . (4) is known as cherzy's borinnula. Thus the loss of head due to bruiction in a in pipe from cherzy's foremula can be obtained it the velocity of the mough pipe and also the value of C is known. The value of m fore pipe is always equal to an algo it.

MINOR ENERGY (HEAD) LOSSES 7

The toss of head on energy due to prinction in a pripe is known as major loss while the loss of energy, due to change of velocity of the bollowing blued in magnitude on direction is called minor boss of energy. The minor loss of energy (or head) includes the bollowing cases:

- 1. Loss of head due to dudden enlargement,
- 2. Loss of head due to sudden contraction,
- 3. Loss of head and the entrance of a pipe
- 4. Loss of head of the exit of a pipe
- 5. Loss of head due to an obstruction in a pipe,
- 6. Loss of head alue to bend in the pipe,
- 7. Loss of head in Nanious pipe bittings.
- In case of long pipe the above losses are smallies compared with the loss of head due to briction and hence they are called minor tosses and even may be neglected without serious error But in case of a short pipe, these losses are comparable with the loss of head due to friction.

HYDRAULIC GRADIENT AND TOTAL ENERGY LINE ?

The concept of hydroculic gradient line and total energy line is very useful in the study of the blow of thirds through Pipe They are defined as: Hydroculic Gradient Line of

It is defined as the line which gives the sum of pressiving. Head (P) and datum head (Z) of a flowing bluid in a pope with respect to some reference line or it is the line which is obtained by Joining the top of all ventral ordinates, showing the pressure head (p) w) of a flowing bluid in a pipe pressure head (p) w) of a flowing bluid in a pipe pressure head (p) w) of a flowing bluid in a pipe is mom the centre of the pipe It is briefly written as H.G.L. (Hydraulic Gradient Line).

Potal Energy Line 7

It is defined as the time which gives the sum of pressure head, datum head and kinetic head of a blowing blund in a pipe with respect to some reference line. It is also defined as as the line which is obtained by Joining the tops of all verdical Dirdinates' showing the sum of pressure head and kinetic head from the centre of the pipe. It is briefly wratter as T.E.L. (Total Energy Line).

F.M

Introduction 7

The liquid comes but in the borm, of a Set brown the outlet The liquid comes but in the borm, of a Set brown the outlet of a nozzle, which is time bitted to a pipe through which the thirt. liquid is blowing under pressure. It some plate, which may be fixed on moving, is placed in the path of the jet, a force is exercised by the jet on the plate. This bouce is obtained brown Newton's and law of motion or from impulse-momentum equation. Thus impact of jet means the force exercised by the jet on a plate which may be stationary on moving. In this chapter, the following cases of the impact of jet the the force exercised by the jet on a plate, will be considered.

ECHAPTER-073

(d) Fonce exercised by the set on a stationary plate when (a) plate is viercifical to set

(b) plate is inclined to the jet, and it is in

(?) Fonce exercted by the set on a moving plate, when (?) Fonce exercted by the set on a moving plate, when

(b) plate is inclined to the Jet and

(c) plate is curved,

Monce Exercted By The Jet On a stationary Ventical Plate 7

Gonsider a jet of water coming out from the norrele, strukes a blat vertical plate as shown in the below figure.

PIPE NOZZLE NOZZLE JET OF THE WATTER

(Force exercised by set on ventical plate) :

Let V = velocity of the jet

d = diaminitian of the jet $a = anea of Chois section of the jet = <math>\frac{\pi}{4} d^2$

The jet abten striking the plate, will move along the plate: But the plate is at night angles to the jet. Hence the jet abten to Striking, will get deflected through 90°. Hence the component of the velocity of jet in the direction of jet, abten striking will be zerop.

The bonce exercted by the set on the plate in the direction of set.

Fx = Rate of change of momentum in the direction of bonce

Initial momentum - Final momentum

- (Mass x Initial velocity - Mass x Final velocity) . Time - Mass (Initial velocity-Final velocity) = $(Mass/sec) \times (Velocity of jet before streiking$ = <math>PaV(V-0) ("mass/sec = PxaV) = PaV^2 (1) = fav? Fonce Exercted by a jet on stationary, Cureved, plate > (+) let strikes the curried plate out the centre !-Let a jet of water strickes a bixed curved plate at the Centre as shown in the below strigune. The Set abten striking the plate, comes out with the same velocity. It the plate is smooth and there is no loss of energy due to impact of the jet, in the one tangential direction of the curved plade. The velocity at outlet of the plate can be resolved that two composients. One in the direction of jet and other perpendicular to the dinection of the Jet. components of velocity in the dimection of let = - V cos of Vy Vsino V Cose Fixed Curved plate

(Jet striking a bixed curved plate at centre)

(-ve sign is taken as the velocity at outlet is in the opposite direction of the set of water coming out from Nozzle). Component of velocity perpendicular to the set = V son a Forced exerted by the set in the direction of set, Fx = mass per sec × [V1x - V2x] where , Vix = Initial velocity in the direction of viet = V Vax = Final velocity in the direction of jet = - VCosa · Ex = Pav[v-(-vcoso)] ··· = Pav [V+ vcoc o] - (3) = = fan2[1+ cos 0] Similarly + Fy = mass part lec × 24 V2Y - V2Y where i Vily = Entitlat velocity in the done of on ob. Y = D Vay = Finial velocity in the direction of Y = Vsino . $F_{y} = f_{a}v_{b} - v_{sino} - \omega$. FRE-favesing & -ve sign means that force is acting in the downward director. In this case the angle of deflection of jet = (180°-0) (B) Jet Strukes the Curved plate at one end tangentially when the plate is symmetrical :-Left the Set Stadker the Curved biked plate at one end & tangentially as shown in bigance. Let the curved plate is symmetrical about strainis. Then the angle made by the trangents at the two ends of the plate will be scine.

NY JUSINO Let V = velocity of jet of water O= Angle made by let with x-axis V COS O Cunved Plate at inlet tip of the curved plates Stathe Plate is smooth and loss of energy due to impact is Zeno, JET VCOSO then the velocity of water & at the outlet tip of the curved plate will be equial to V. The forces exercised by the Jet of volter. in the dimensions of a and y are Fx = (mass /sec) x [Vix - Vax] = fa V[V coso - (- V coso)] Jet struking Curved bixed plate at one end = fa V[vcoso + vcoso] = 2 fav2 coso - (4)

 $F_{y} = faV[V_{iy} - V_{ay}]$ = faV[V_{sing} - V_{sing}] = 0

(C) Jet stackes the Curved plate at one end tangentially when the plate is unsymmetrical :-

When the Curved plate is unsymmetrical about X-axos, then t angle made by the tangents dreawn at the inlet and outlet tips of the plate with x-axis, will be applicated.

Let $\Theta = angle made by tangent at inlet tip with X-axis.$ $<math>\Phi = angle made by tangent at outlet tip with X-axis$ The two components of the velocity out inlet serve

· Vix = V cos & and . Viy = . Vsin Q ...

Force or the Curry'ed plate when the plate is moving in the direction of jet ;-

Let a jet of water strukes a curved plate at the Centre of the plate which is moving with a unitorm velocity in the direction of the jet as shown in the figure.

(V-u) Cos o

Alv-u) sino

Let V = Mosolute velocity of jet a = anea of jet u = velocity of the plate in the dimention of the jet (Jet striking a Curved moving)

The velocity with which jet strikes the curved plate = (V-u).

- It plate is smooth and the loss of energy due to impact of jet is zero, then the velocity with which the jet will be the leaving the curved vane = (V-u).

- This velocity can be restored into two components, one in the direction of the set and other perpendicular to the direction of the set

component of the velocity in the direction of silet

- (re sign is taken as at the outlet, the component is in the opposite direction of the jet).
- Component of the velocity in the direction perchandicular to the direction of the let = $(V-u) \sin \theta$
- Mass of the water struking the plate. = fx a x velocity with which jet strukes the plate = fxa(V-W).
- : Fonce exercised by the jet of water on the curved plate in the direction of the jet,
 - Fy = mose stacking pensec X [Enotical velocity with which bet stackes the plate in the direction of wet - Final velocity]
 - $= fa(v-u)[(v-u)-(-(v-u)\cos \omega)]$ = fa(v-u)[(v-u)+(v-u)\cos \omega] = fa(v-u)?[(1+\cos \omega)] (9)
- Wonkdone by the jest on the plate perc second
 - = Fx X Distance travelled per second in the direction = Fx X u

(10)

Search and a search and

= fa(v-u)2[1+ cos o]u = fa(v-u)2 x u[1+ cos o] -

Sec. 11

3 8 -

Fonce Exended by a set of Water on an Unsymmetricy Moving Cureved plate a when set strukes Tangentially at one of the Tips of 4 42-11 Vw214 4 - u (Cuinved Vane at one of the tops) A TX TO T. D.

The above figure shows a jet of , water struking a moving curved plate (also called vane) tangentially, at one of its tips; As the jet Strukes tangentially, the loss of eneorgy due to impact of the jet will be zero. In this case as plate is moving the velocity with which jet of water strukes is equal to the relative velocity of the jet with respect to the plate. Also as the plate is moving in different direction of the jet, the relative velocity at inlet will be equal to the weetore difference of the velocity of the jet as and velocity of the plate at inlet. Let V1 = Velocity of the set at inlet , u1 = Velocity of the plate (Vaine) at inlet Virs = Relative velocity of jet and place and inlet or= Angle between the direction of the set and direction of motion of the plate, also called guide blades angle O = Angle made by the relative velocity (Vrg) with the derection of motion at inlet also called vane angle at inlet Vive and Viri = The components of the velocity of the set Vi, in the dimetion of motion and percendicular to the direction of motion of the Vane respectively Vw1 = It is also known as velocity of white at inlet V51 = It is cuso known as velocity of blow at inlet V2 = velocity of the set, leaving the vane or velocity of set at outlet of the vane. lez = Nelocity of the Vane at putlet VK2 = Relative velocity of jet with respect to the vane at outlet B = Angle made by the velocity N2 with the direction of motion of the vane at outlet. \$= Angle made by the relative velocity (Vn2) with the direction of motion of the Name of Outlet and also becalled vane angle at outlet Vwz and V52 = components of the velocity Vz, in the direction of motion of vane and perpendicular to the direction of motion of vane at outlet Vwe = It is also called the velocity of whird at outlet

" Voz = Velocity of blow at outlet

The trivingles ABD and EGH are called the velocity trivingles at inlet and outlet. These velocity triangles are drawn as given below :-

(1) Velocity Triangle at Inlet :-.

Take any point A and draw a line AB = V2 in the magnitude and direction which means line AB makes an angle of with the horizontal line AD. Next draw a line AC = 44 in magnitude. Join C to B. Then CB represents the relative velocity of the set at inlet. It the loss als energy at inlet due to impact is zero, then CB must be in the targentical direction the the vane at inler. From B draw a ventical line BD in the dward direction to meet the horizontal Bline AC produced at D.

Then BD = Represents the Velocity of blow out inlet = Vs1 AD = Represents the Velocity of which entinlet = Viel LBCD = Vane angle at inlet = D LBAC = X

(3) Velocity Triangle at Outlest :-

It the vane Surface is assumed to be very smooth, the loss of energy due to traction will be zero. The water with be gloding on over the Surface of the vane with a relative velocity equal to Var and will come out of the vane with a relative velocity very this means that the relative velocity at surflet Var = Var. And also the relative velocity of outlet should be in tangential draction to the Vane of outlet. Drup Ely in the tungential direction of the Vane at Dutlest and out Ely = Vice. from by draw a line GF in the dimension of vane at outlet and equal to uz, the velocity of the Vane at outlet. Join EF, then EF represents the absolute velocity of the jet at outlet in magnitude and direction. From E draw a the verdical line EH to meet the line 4F produced at H. Then EH = velocity of blow of budlet = V62 FH = velocity of whind at outlet = Vioz LEGF= \$ = Angle of the Vane of our let ZEFH = B = Angle made by V2 with the direction of motion of Vane of outlet. It-the vane is smooth and is having velocity in the direction of motion at inlet and outled equal then we have. 4 = uz = u = - Nelocity of vane ' in the direction of motion . and Vrey = Vrez . Now mak of worder stricking wane per sec = faving - co where a = Area of Jest of water Vr. = Relative Vehocity at inlet :. Fonce exerted by withe set in the direction of motion Fx=mall of wooden striking per sec. X (Instead velocity with respect to which set stables in the direction of motion - Final velocity of . Set in the direction of motion] But noted velocity with which Jet the strokes the vane = Vict (3) this velocity in the direction of motion The component of = Vici Loso = (Vivi, - m)

Similarly, the components of the relative velocity at outled in with a direction of motion = - Vac Los of

$$= -[u_2 + V_{02}]$$

-ve sign is taken as the component of Vicz in the direction of motion is in the opposite datection.

Substituting the equation (1) and all above values of the velocities in equation (2), we get

Equation (3) is true only when angle B shown in Bigure is an acute angle. It B= 90°, the Vivz = D, then equation (3) becomes as, Fx = favri [Vwi]

It Bis an obtage angle, the expression box Fx will become

Fx = Pa Vry [Nov Vwg - Nw2] Thus in general, Fx is written as Fx = favri [Vwit Vw2]

Work done per second on the Name by the jet

= Fonce & Distance por second in the denection of tonce. = Fx X W

$$= \operatorname{fav}_{w_1} [v_{w_1} \pm V_{w_2}] \times u = (4)$$

". Workdone per second per unit weight of bluid striking per

(3) Efficiency of JET ?

The work done by the Set on the vane given by equation (4) is the output of the Set where as the initial kinetic energy of the set is the input. Hence, the efficiency (91) of the set is expressed as

where m=mass of the bluid per second in the jet = fav, V1 = initial velocity of jet :. M= favry [Vw1 ± Vw2] xu V2(Pav1) x v1²
(7)

MODEL SET QUESTION PAPER FOR PRACTICE SET-1

Semester:4th

Branch:Mechanical Engineering

Subject Name: Fluid Mechanics

Full Marks- 80

Time- 3 Hrs

Answer any five Questions including Q No.1& 2 Figures in the right hand margin indicates marks

	Answer All questions	2 x 10
a.	Define Mass Density. What is its unit?	
b.	Define the term Kinematic Viscosity. State its SI unit.	
с.	State Archimede's Principle.	
d.	What do you mean by Surface Tension? State the expression for Surface	
	Tension on a hollow bubble.	
e.	What is mean by Vaccum pressure and Atmospheric pressure?	
f.	Define Buoyancy.	
g.	What do you mean by Metacentre?	
h.	Define uniform and non-uniform flow.	
i.	Define Pitot Tube.	
j.	What is meant by Total Energy Line?	
	Answer Any Six Questions	5 x 6
a.	Derive the expression for Capillarity Fall.	
b.	Derive the expression for rate of flow through venturimeter.	
с.	Classify Notch into its different categories.	
d.	What are the Different Losses of energy in pipes? State the Darcy Weisbach	
	Formula for head loss.	
e.		
f.		
	_	
g.	Write a short note on "Differential Manometers"	
	Derive the force exerted by a jet in the direction of the jet on a moving	10
		10
		10
	-	
	b. c. d. e. f. g. h. i. j. d. c. d. e. f.	 a. Define Mass Density. What is its unit? b. Define the term Kinematic Viscosity. State its SI unit. c. State Archimede's Principle. d. What do you mean by Surface Tension? State the expression for Surface Tension on a hollow bubble. e. What is mean by Vaccum pressure and Atmospheric pressure? f. Define Buoyancy. g. What do you mean by Metacentre? h. Define uniform and non-uniform flow. i. Define Pitot Tube. j. What is meant by Total Energy Line? Answer Any Six Questions a. Derive the expression for Capillarity Fall. b. Derive the expression for rate of flow through venturimeter. c. Classify Notch into its different categories. d. What are the Different Losses of energy in pipes? State the Darcy Weisbach Formula for head loss. e. The diameter of a pipe at the section 1 and 2 are 10cm and 15cm respectively. Find the discharge through the pipe if the velocity of water flowing through the pipe at section 1 is 5cm. Find the velocity at section 2. f. A plate 0.025mm distant from a fixed plate, moves at 60cm/s and requires a force of 2N/m² to maintain this speed. Determine the viscosity of fluid between the plates.

5	State and derive the Bernoulli's theorem for steady flow for an incompressible	10
	fluid. What are the assumptions made in the derivation of Bernoulli's equation?	
6	A rectangular plane surface is 2m wide and 3m deep. It lies in vertical plane in	10
	water. Determine the total pressure and position of center of pressure on the	
	plane surface when its upper edge is horizontal and	
	I. Coincides with the water surface.	
	II. 2.5m below the free water surface.	
7	A jet of water 40mm diameter moving with a velocity of 120m/s impinging on	10
	a series of vanes moving with a velocity of 5m/s. Find the force exerted,	
	workdone and efficiency.	

MODEL SET QUESTION PAPER FOR PRACTICE SET-2

Semester:4th

Branch:Mechanical Engineering

Subject Name: Fluid Mechanics

Full Marks- 80

Time- 3 Hrs

Answer any five Questions including Q No.1& 2 Figures in the right hand margin indicates marks

1.		Answer All questions	2 x 10
	a.	Define Weight Density. What is its unit?	
	b.	What do you understand by Continuity Equation?	
	c.	What do you mean by Capillarity?	
	d.	What do you mean by Surface Tension? State the expression for Surface	
		Tension on a liquid jet.	
	e.	What is mean by Absolute pressure and Gauge pressure?	
	f.	What are the assumptions made in the derivation of Bernoulli's equation?	
	g.	What do you mean by Metacentric Height?	
	h.	Define steady and unsteady flow.	
	i.	Define Orifice.	
	j.	What is meant by Hydraulic Gradient Line?	
2.		Answer Any Six Questions	5 x 6
	a.	Derive the expression for Capillarity Rise.	
	b.	Derive the pressure expression for a inverted differential U-Tube Manometer.	
	c.	Define Pitot tube. Derive the expression of velocity at a point using Pitot Tube.	
	d.	Derive the discharge over a Rectangular Notch.	
	e.	What are the guage pressure and absolute pressure at a point 3m below the free	
		surface of a liquid having a density of 1.53×10^3 kg/m ³ . Given that the	
		atmospheric pressue is 750mm of mercury, the specific gravity of mercury is	
		13.6 and density of water is 1000 kg/m ³ .	
	f.	A solid cylinder of diameter 4m has a height of 3m. Find the metacentric height	
		of the cylinder when it is floating in water with its axis vertical. The specific	
		gravity of the cylinder is 0.6.	
	g.	State and derive the Pascal's Law.	
3		Derive the following for a moving unsymmetric curved plate when the jet	10
		strikes tangentially at one end of the plate:	
		I. force exerted by a jet in the direction of the jet.	
		II. work done per second per unit weight of fluid on the plate.	
		III. Efficiency of the jet.	

4		State the Darcy Weisbach Formula and Chezy's Formula for loss of head.	10
-			10
		Water flows through a pipe of 200mm in diameter and 60m long with a	
		velocity of 2.5m/s. find the head loss due to friction using:	
		I. Darcy's formula where $f = 0.005$	
		II. Chezy's formula where $c = 55$	
5		An oil of specific gravity 0.7 is flowing through a pipe of diameter 300mm at	10
		the late of 500l/s. find the head loss due to friction and power required to	
		maintain the flow foe a length of 1000m. Take kinematic viscocity as 0.29	
		stroke	
6		A pipeline, 300mm in diameter and 3200m long is used to pump up 50 kg/s of	10
		an oil whose density is 950 kg/m ³ and whose kinematic viscosity is 2.1 stokes.	
		The centre of the pipeline at the upper end is 40m above than that at the lower	
		end. The discharge at the upper end is atmospheric. Find the pressure at the	
		lower end and draw the hydraulic gradient line (HGL) and the total energy line	
		(TEL).	
7		State and derive the Bernoulli's theorem for steady flow for an incompressible	10
		fluid. What are the assumptions made in the derivation of Bernoulli's equation?	-
1	1		

MODEL SET QUESTION PAPER FOR PRACTICE SET-3

Semester:4th

Branch:Mechanical Engineering

Subject Name: Fluid Mechanics

Time- 3 Hrs

Full Marks- 80

Answer any five Questions including Q No.1& 2 Figures in the right hand margin indicates marks

1.		Answer All questions	2 x 10
	a.	Define Specific Gravity. What is its unit?	
	b.	Define the term Dynamic Viscosity. State its SI unit.	
	с.	What is mean by Rate of Flow or Discharge?	
	d.	What do you mean by Surface Tension? State the expression for Surface	
		Tension on a water bubble.	
	e.	State the Bernoulli's theorem for steady flow for an incompressible fluid.	
	f.	Define centre of pressure.	
	g.	What do you mean by Bouyancy?	
	h.	Define Laminar and Turbulent flow.	
	i.	Define Venturimeter.	
	j.	State the Chezy's Formula for loss of head.	
2			
2.		Answer Any Six Questions	5 x 6
	a.	State and derive the Pascal's Law.	
	b.	Classify the Hydraulic Coefficients. State the relationship between them.	
	c.	Derive the discharge over a Traingular Notch.	
	d.	Find the discharge of water flowing over a rectangular notch of 2m length	
		when the constant head over the notch is 300 mm . Take Cd= 0.60.	
	e.	Derive the force exerted by a jet in the direction of the jet on a moving	
	6	unsymmetric curved plate. Also derive the work done per second on the plate.	
	f.	Calculate the specific weight, specific mass, specific volume and specific	
		gravity of a liquid having a volume of 6m ³ and weight of 44kN.	
	g.	Write a short note on Bourdon Tube Pressure Guage.	
3		 I. The head of water over an orifice of diameter 40mm is 10m. find the actual discharge and actual velocity of jet at vena contracta. Take C_C = 0.6 and C_d = 0.98. II. The discharge over a rectangular notch is 0.135m³/s when the water level is 22.5m above the still. If the coefficient of discharge is 0.6, find the length of the notch. 	10
4		I. Describe Hydraulic Gradient Line and Total Energy Line.II. Derive the continuity equation.	10

5	Define Metacenter and Metacentric Height. Derive the expression for	10
	Metacentric Height.	
6	Derive the pressure expression of a simple U-Tube manometer. The right limb	10
	of a simple U-tube manometer containing mercury is open to the atmosphere	
	while the left limb is connected to a pipe in which a fluid of specific gravity 0.9	
	is flowing. The centre of the pipe is 12cm below the level of mercury in the	
	right limb. Find the pressure of fluid in the two limbs if the difference of	
	mercury level in the two limbs is 20cm.	
7	A jet of water of diamter 10cm strikes a flat plate normally with a velocity of	10
	15m/s. the plate is moving with the velocity of 6m/s in the direction of the jet	
	and away from the jet. Find:	
	I. The force exerted by the jet on the plate.	
	II. Work done by the jet on the plate per second.	